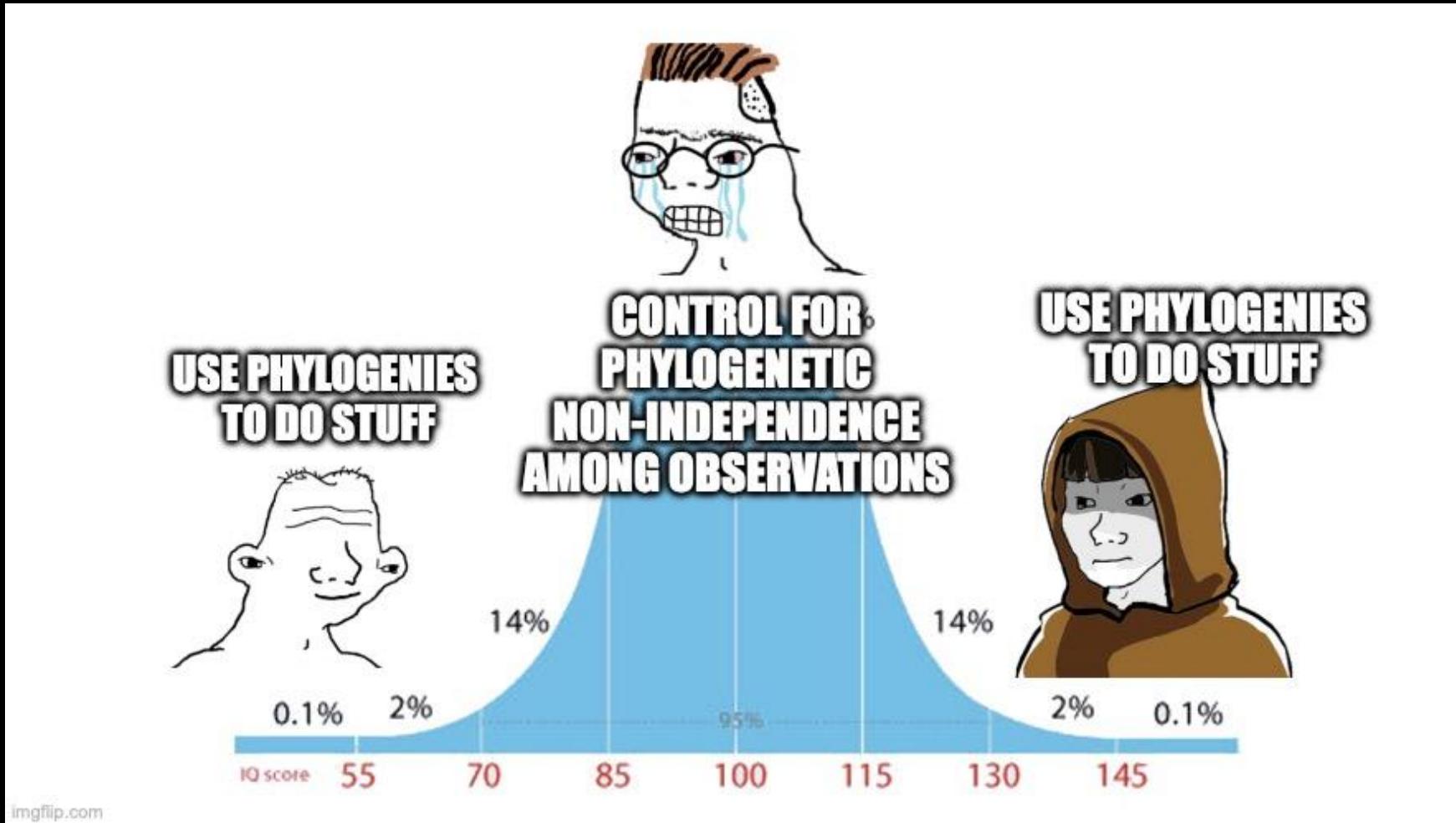


# BEST PRACTICES IN PHYLOGENETIC COMPARATIVE ANALYSES

EQGW 2025

# PHYLOGENETIC COMPARATIVE METHODS



# interpretation



Models

“Estimated data”  
(phylogenies)

Data

# interpretation



Models



inadequacy

“Estimated data”  
(phylogenies)



error/  
inadequacy

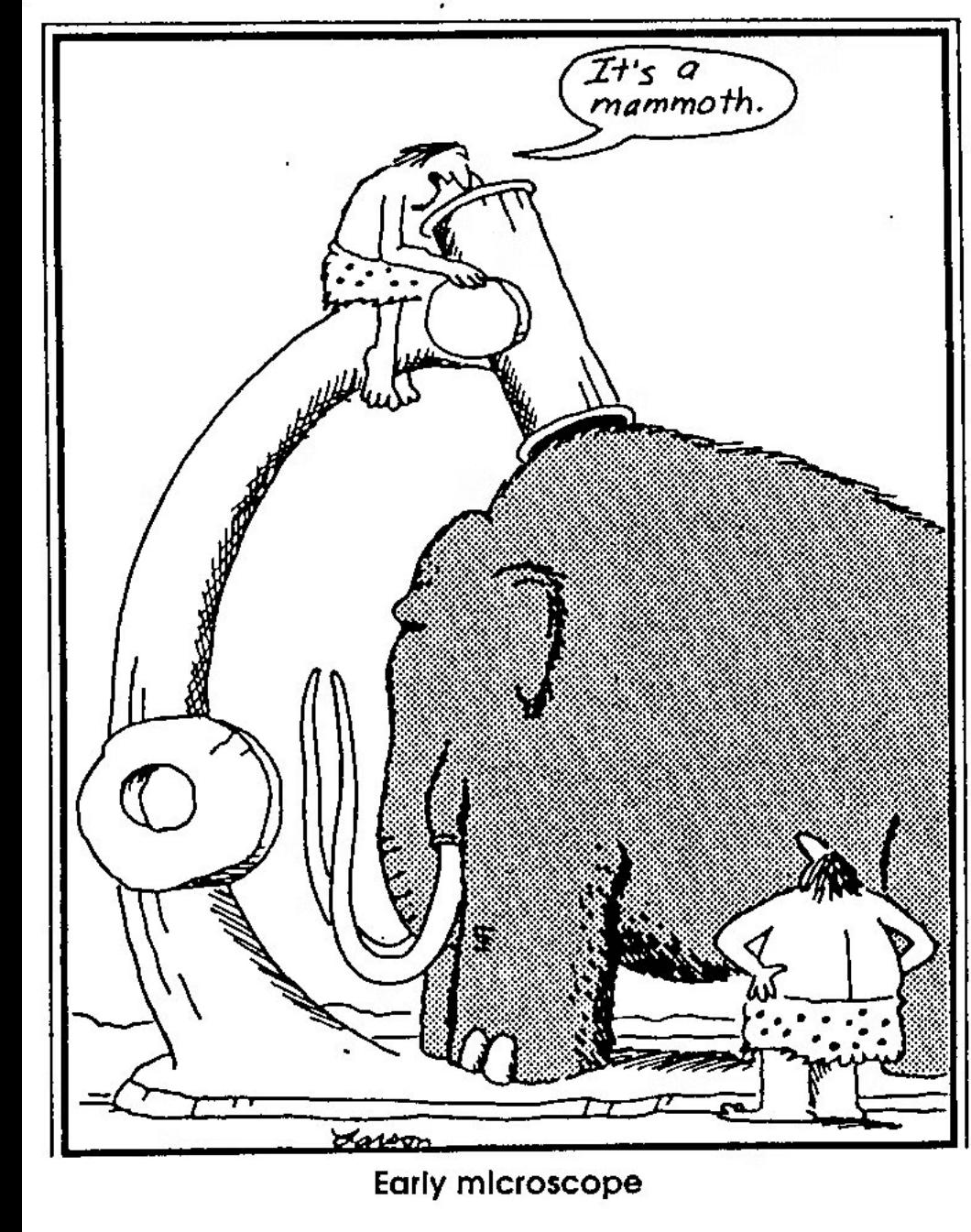
Data



error

# MEASUREMENT ERROR

Measurement errors are not perfect (and sometimes we screw up)



# MEASUREMENT ERROR

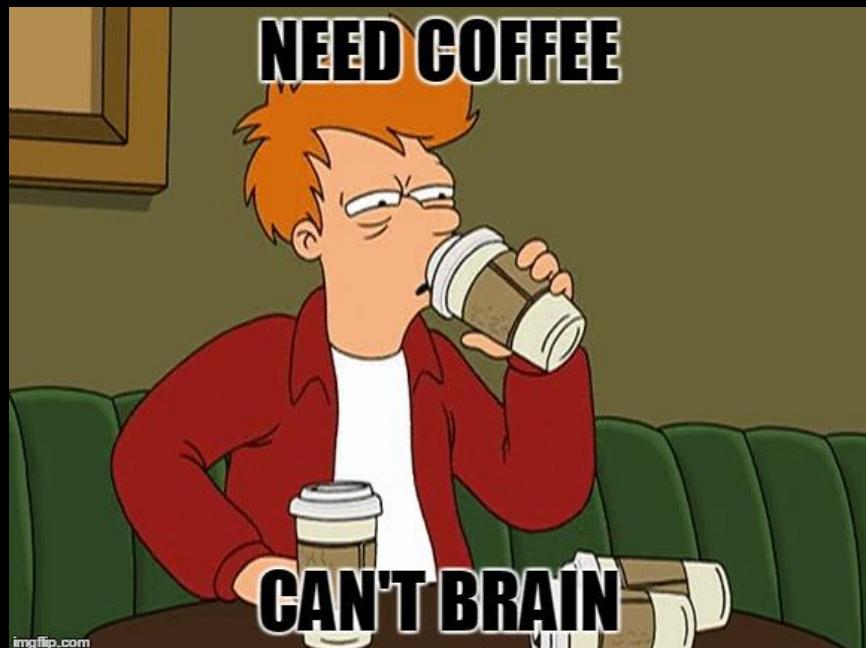
Multiple sources:  
Equipment error/imprecision



# MEASUREMENT ERROR

Multiple sources:

- Equipment error/imprecision
- Interobserver error



# MEASUREMENT ERROR

Multiple sources:

Equipment error/imprecision

Interobserver error

Interobserver error



# MEASUREMENT ERROR

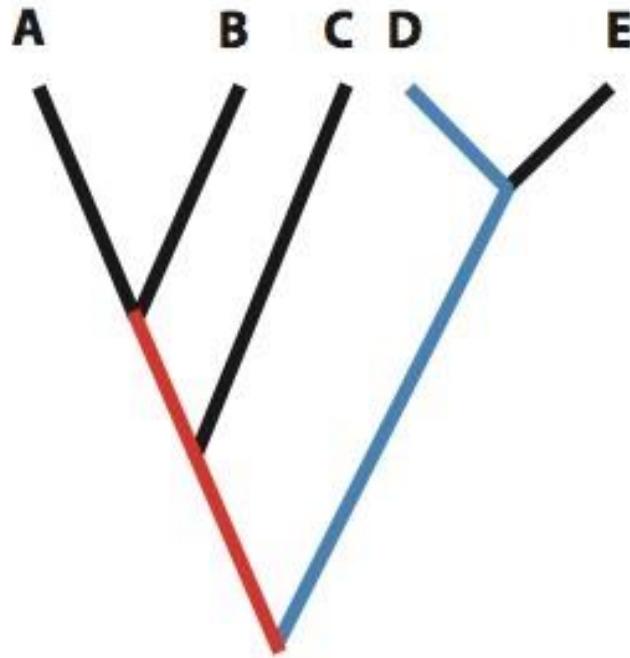
Multiple sources:

- Equipment error/imprecision
- Interobserver error
- Intraindividual- behavior/physiology
- Blocks – treatments
- ...
- etc

Why would it matter in PCM?

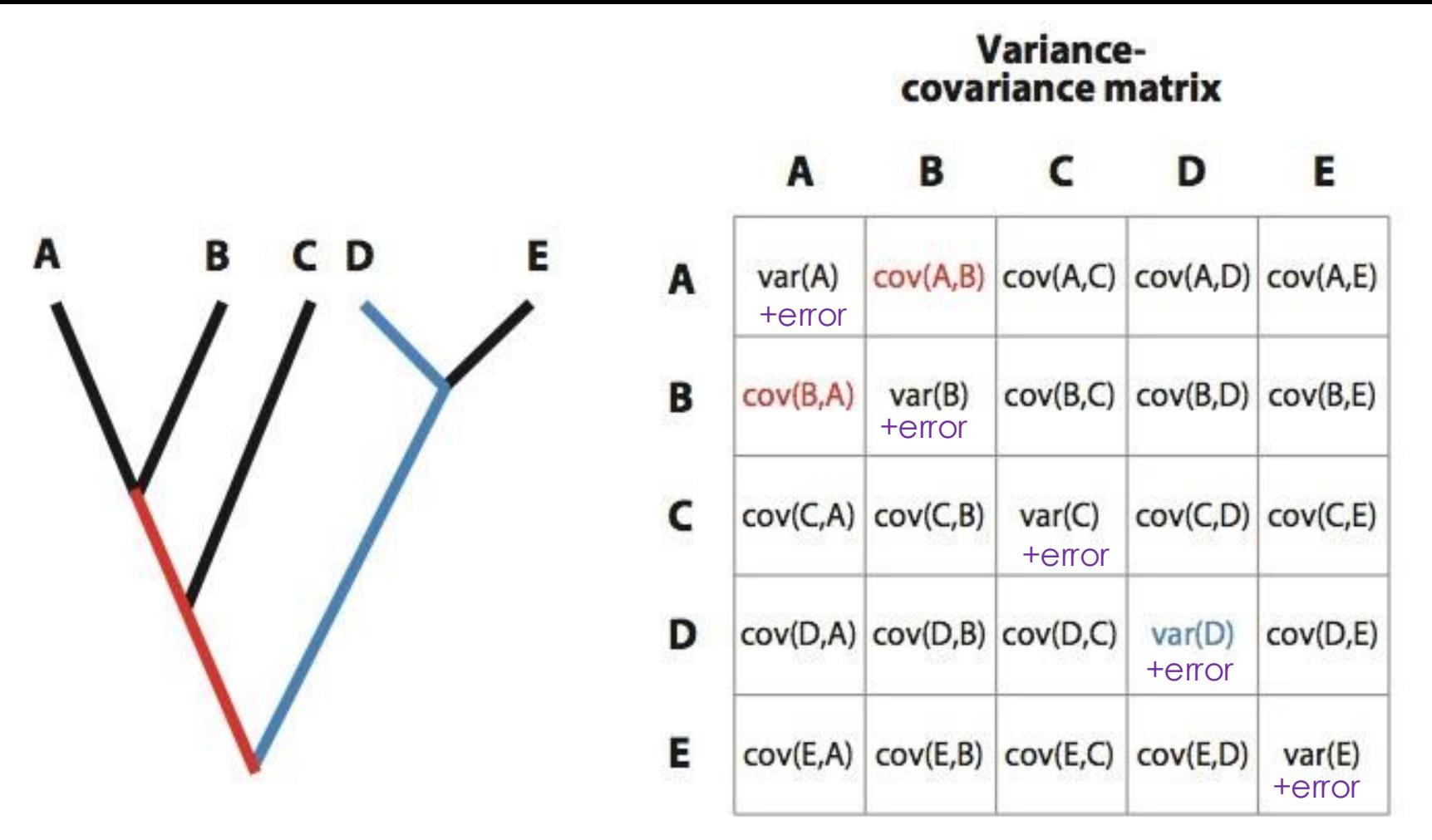


## Variance-covariance matrix

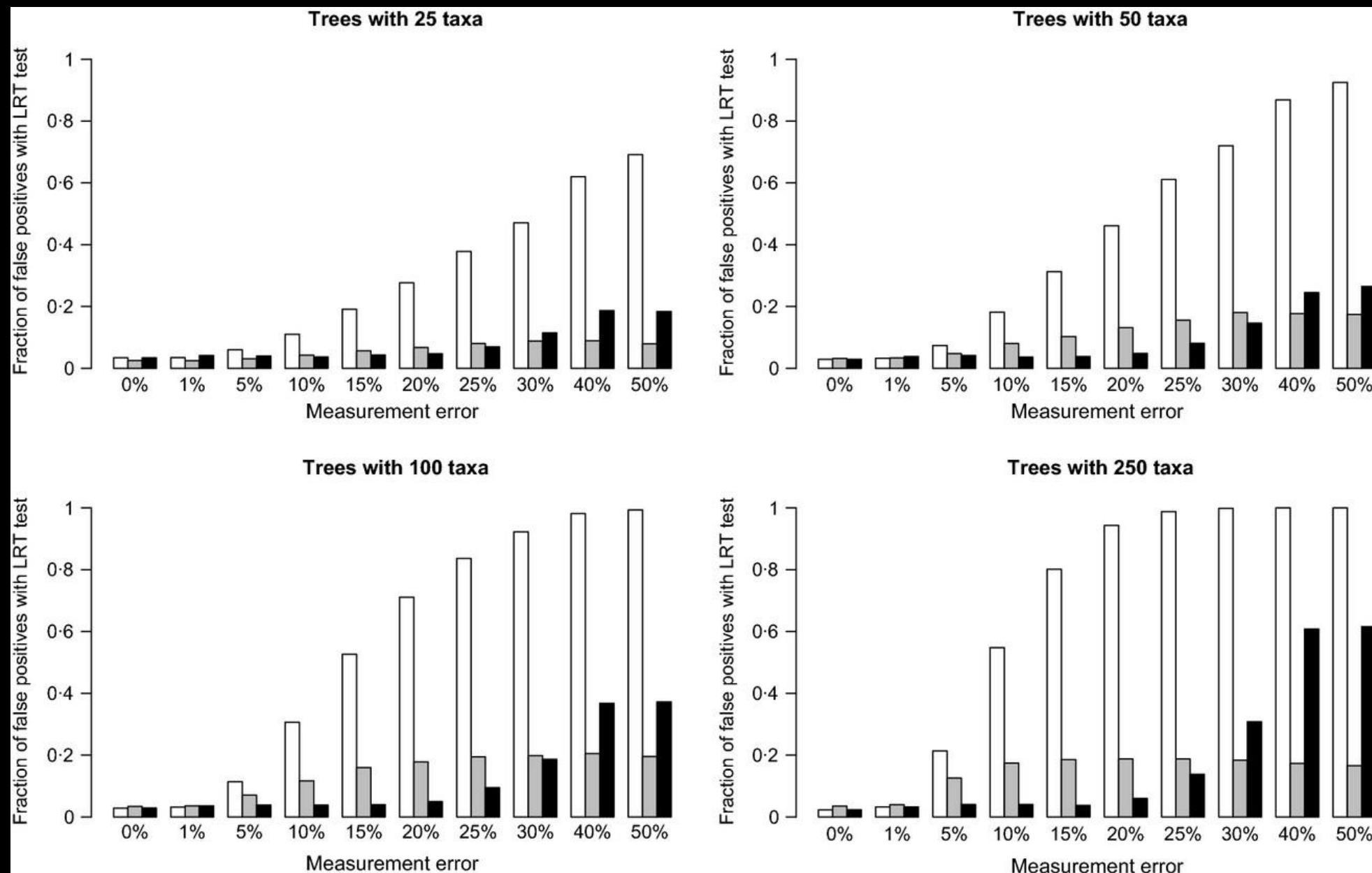


	A	B	C	D	E
A	var(A)	cov(A,B)	cov(A,C)	cov(A,D)	cov(A,E)
B	cov(B,A)	var(B)	cov(B,C)	cov(B,D)	cov(B,E)
C	cov(C,A)	cov(C,B)	var(C)	cov(C,D)	cov(C,E)
D	cov(D,A)	cov(D,B)	cov(D,C)	var(D)	cov(D,E)
E	cov(E,A)	cov(E,B)	cov(E,C)	cov(E,D)	var(E)

If we have error, this is imprecise



Does it matter in reality?



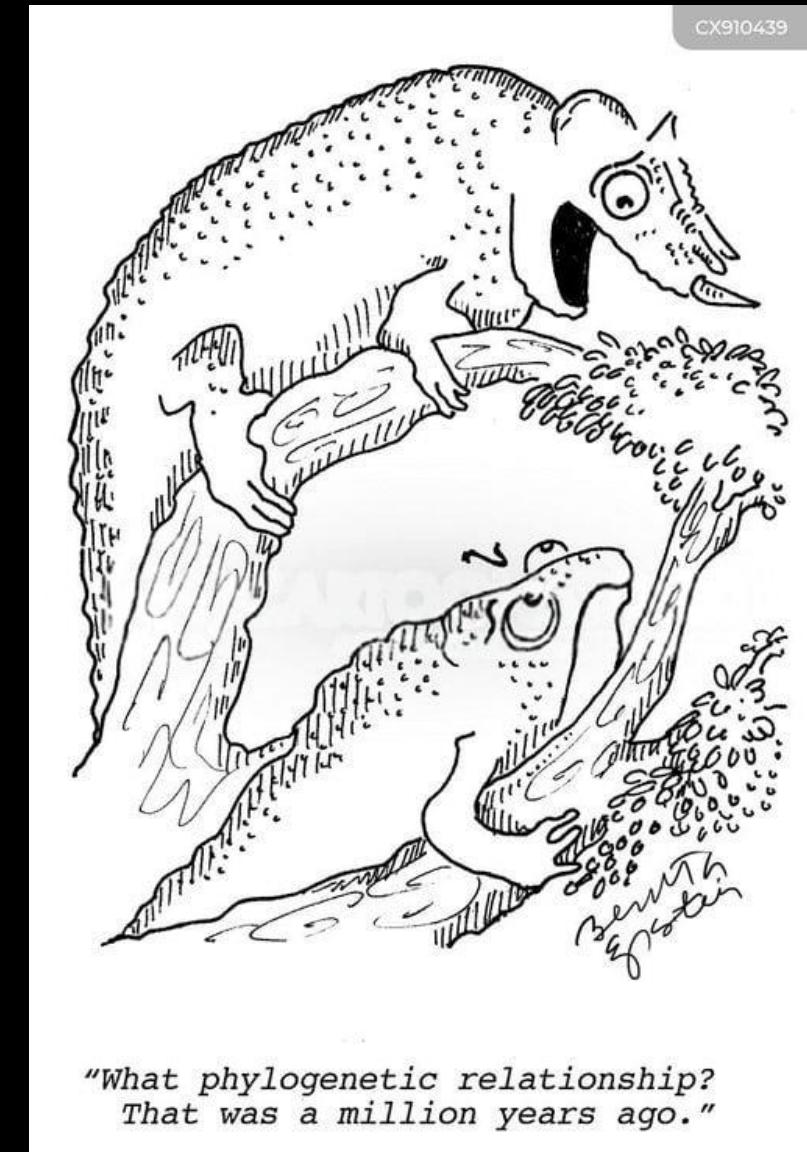
White- ME ignored; Gray- ME estimated; Black- ME known

# LESSONS

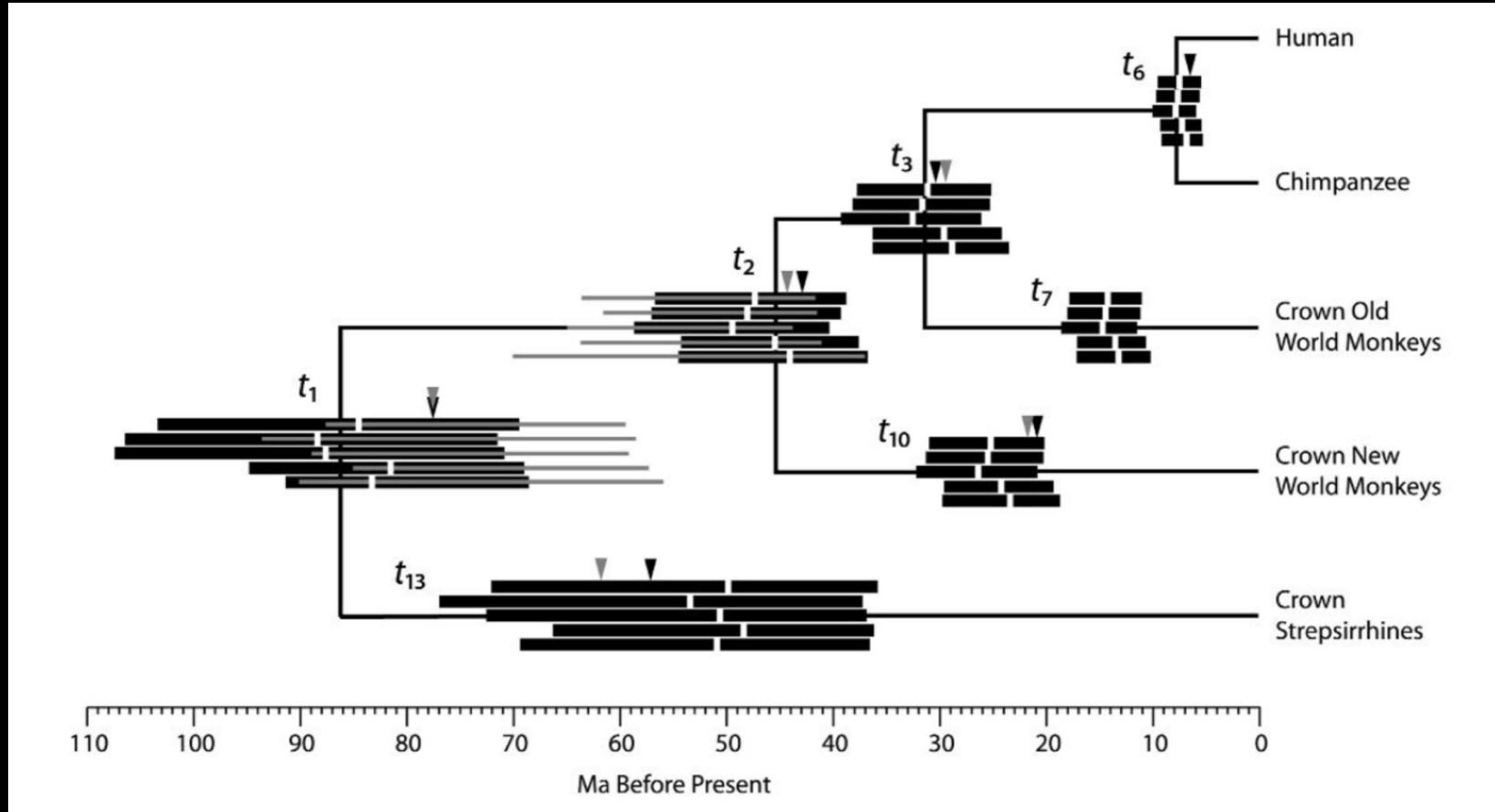
Always account for measurement error

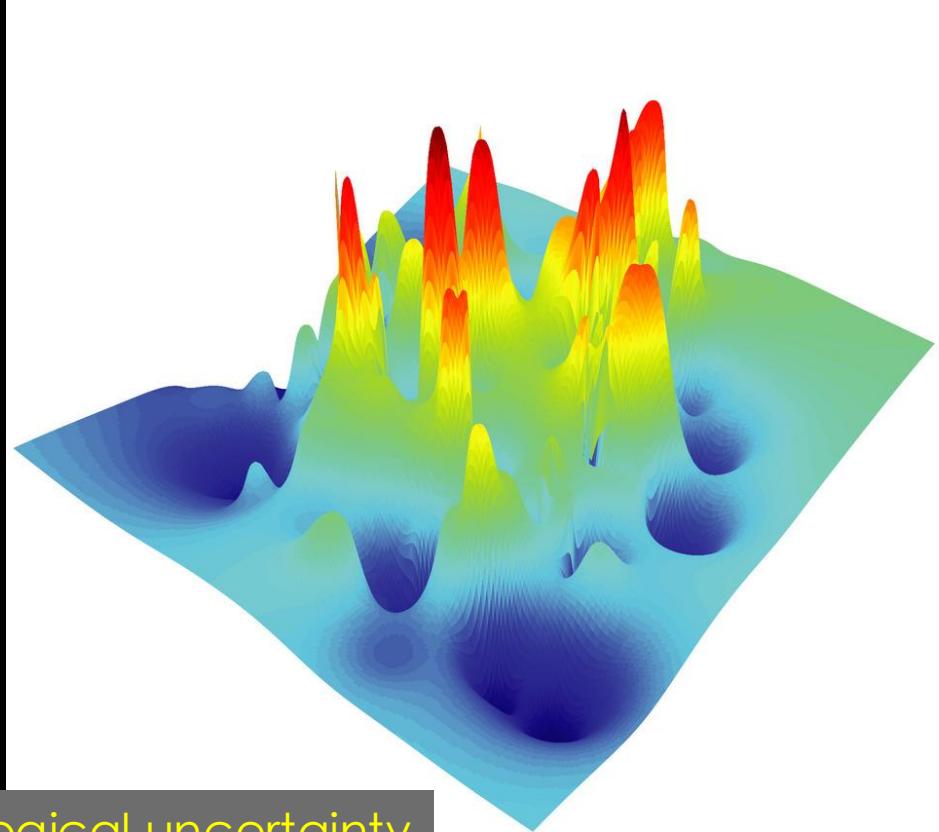
# PHYLOGENETIC UNCERTAINTY

Phylogenies are estimated,  
and therefore have errors  
and uncertainties

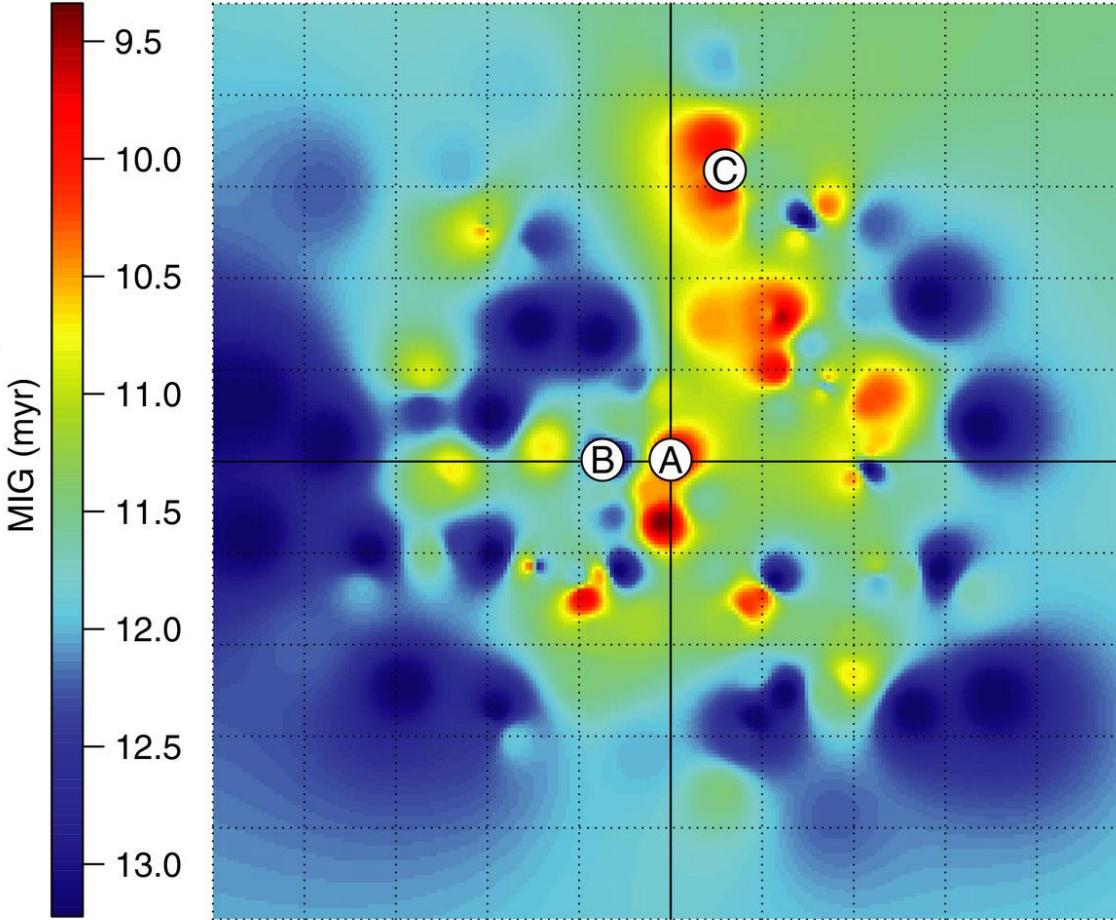


# PHYLOGENETIC UNCERTAINTY

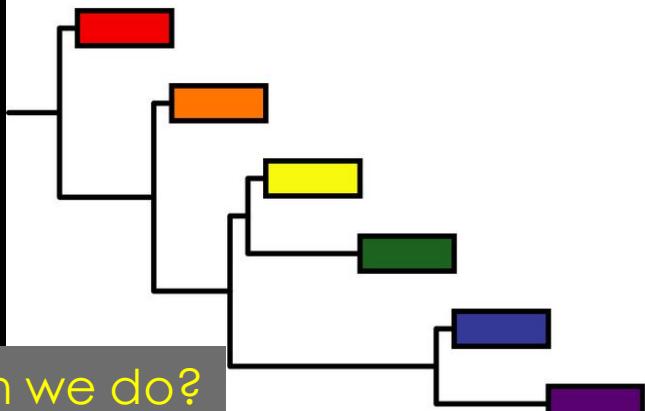




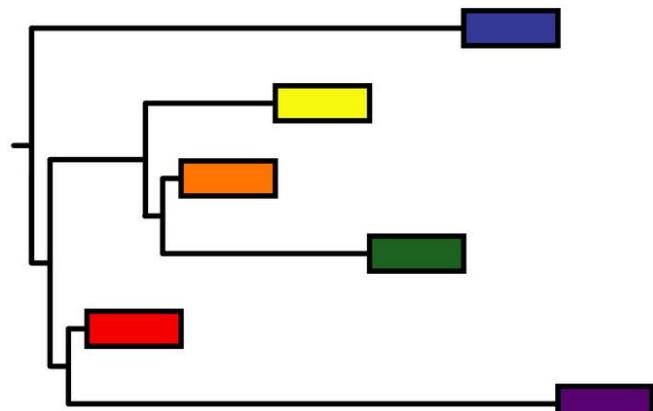
Topological uncertainty



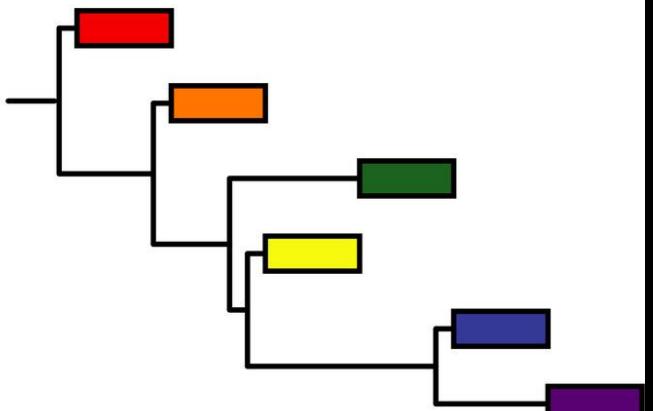
**A** (MIG = 6 myr)



**B** (MIG = 13 myr)

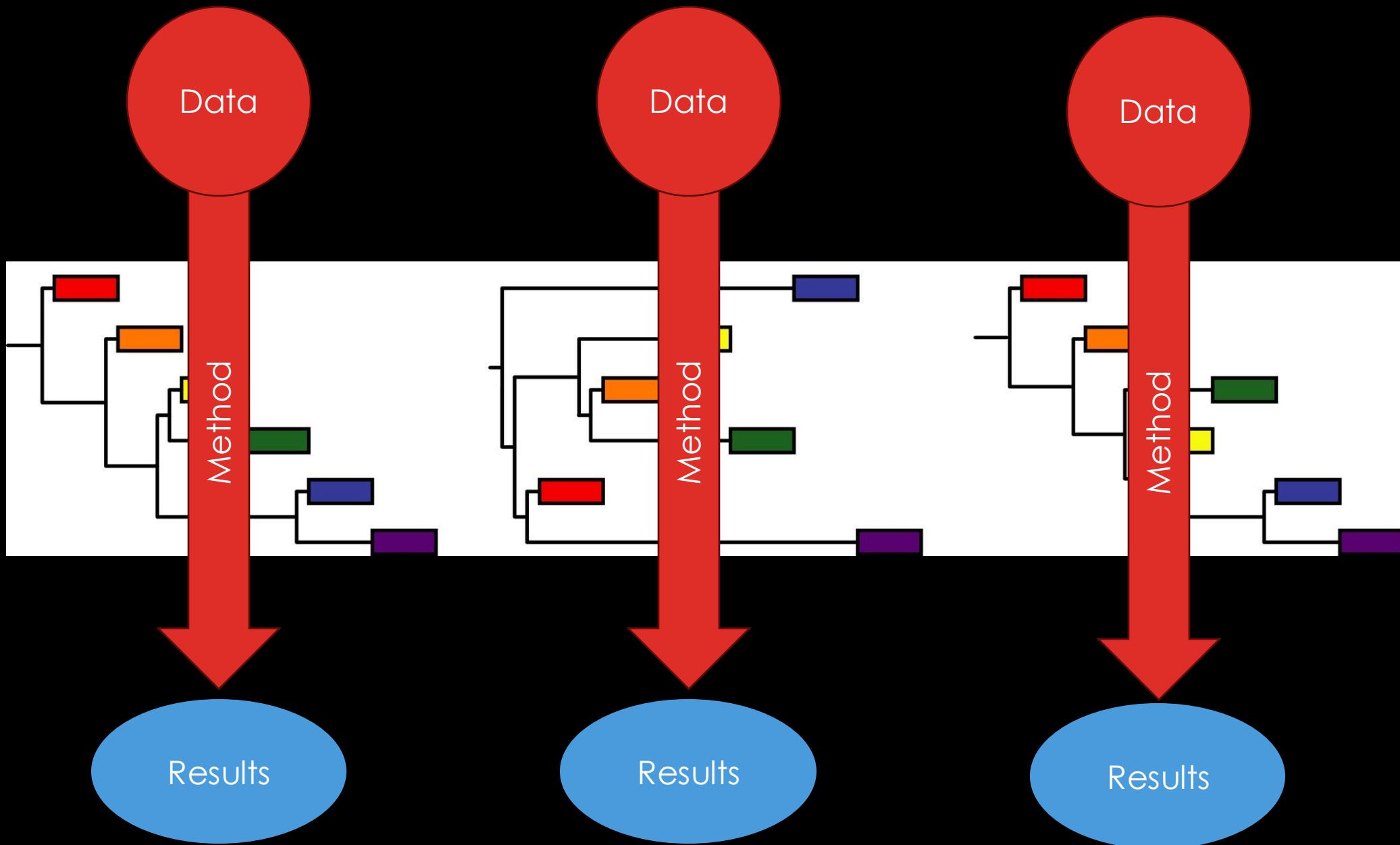


**C** (MIG = 6 myr)

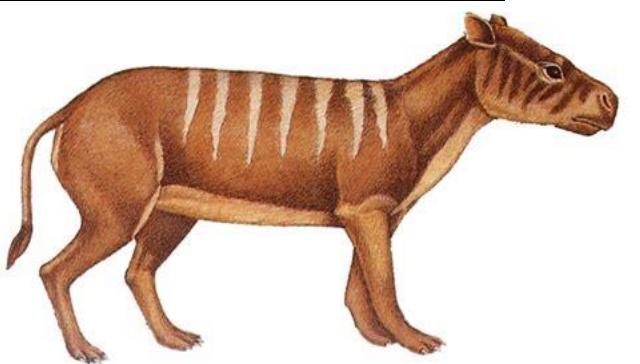


What can we do?

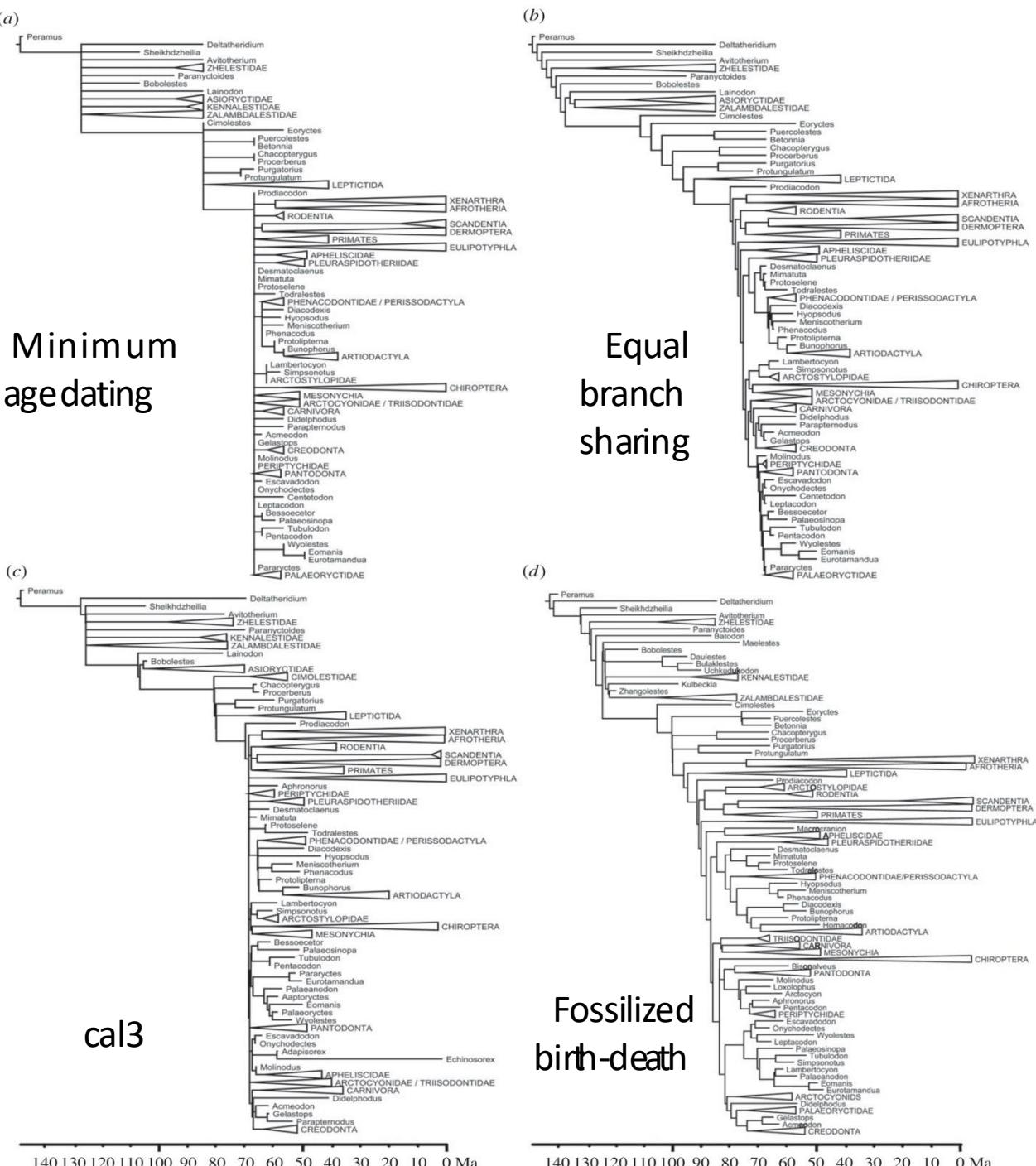
Rerun analysis with a bunch of trees!

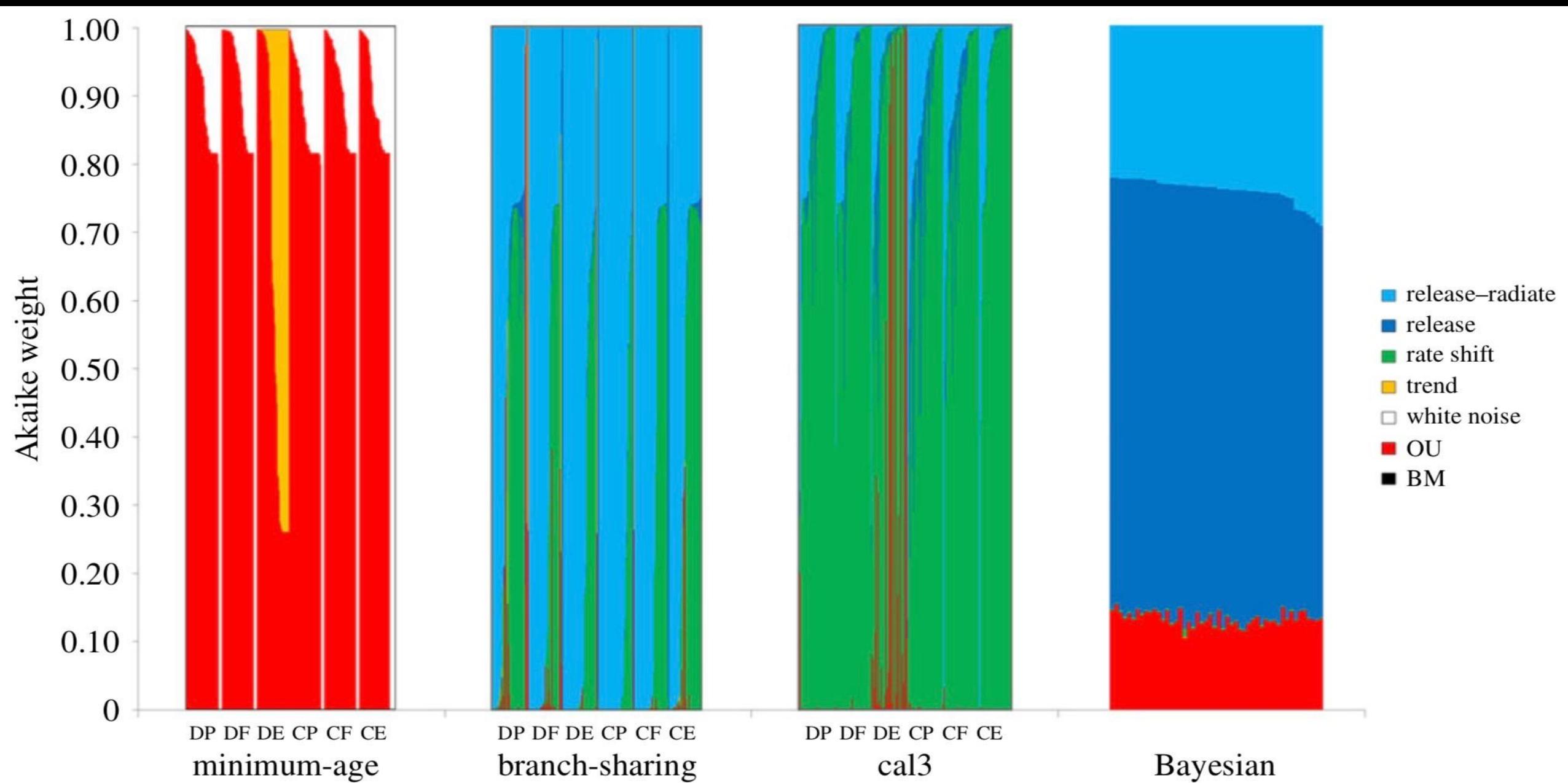


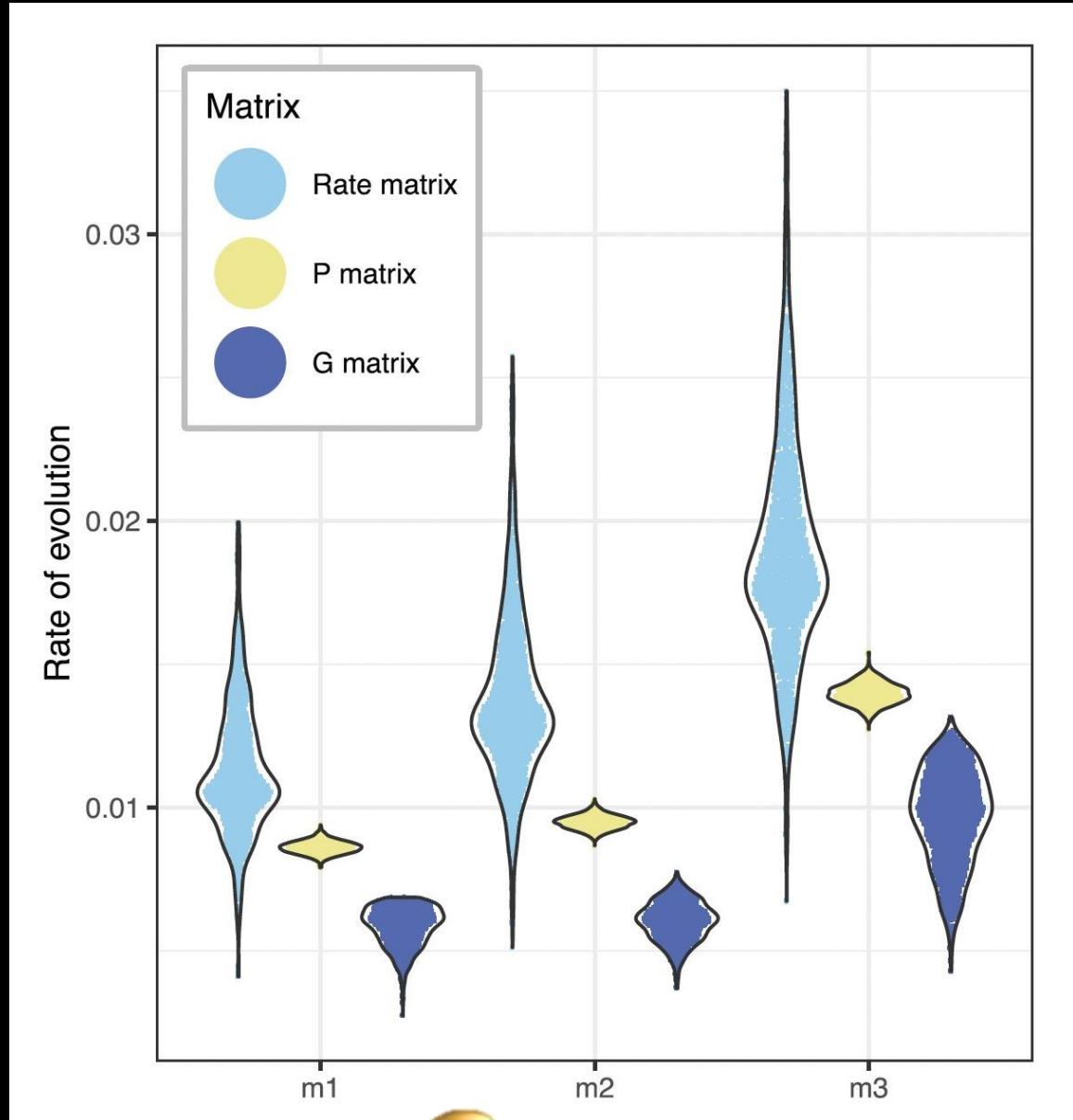
# Body mass evolution in fossil mammals



Halliday & Goswami2016







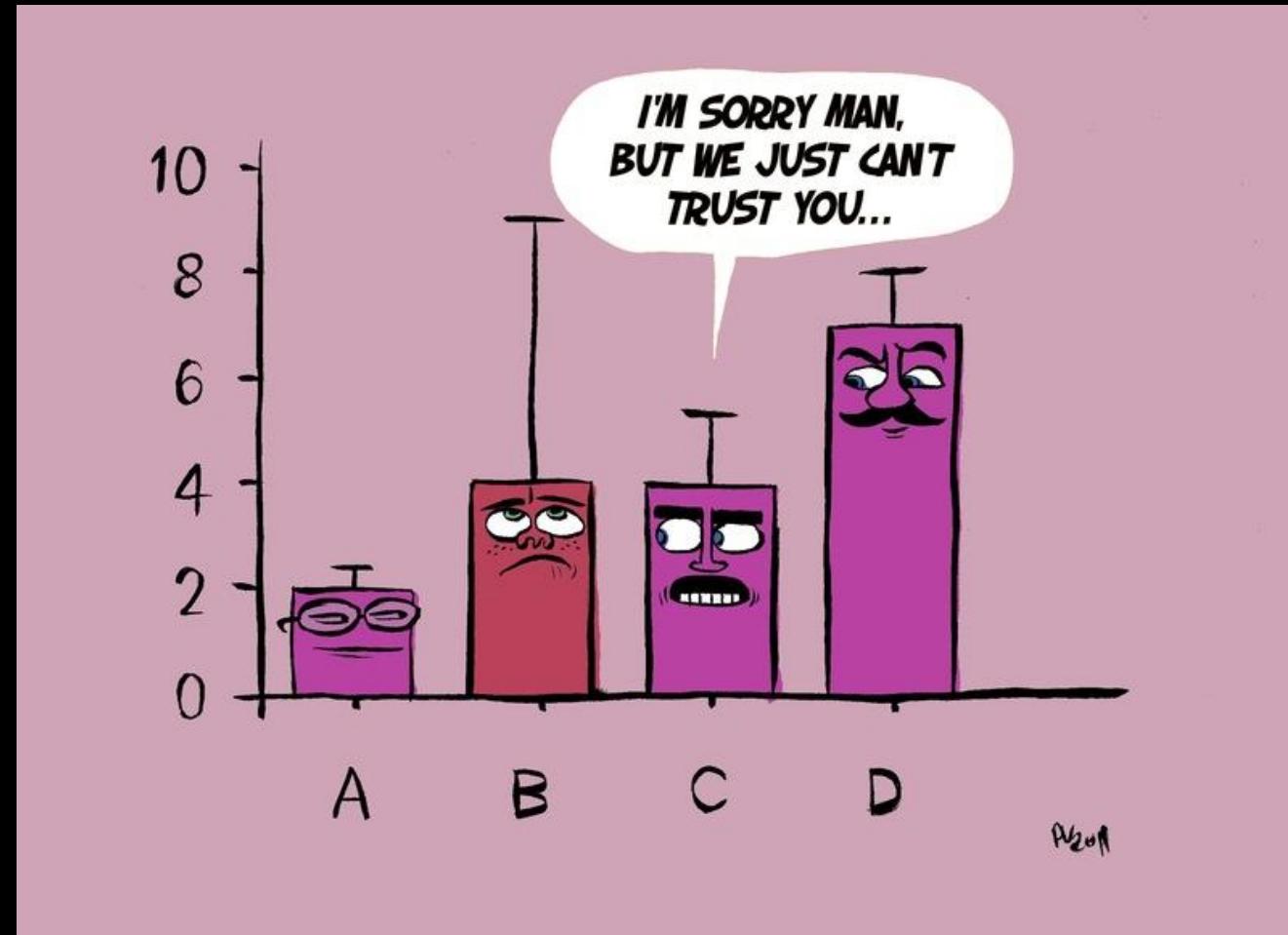
# LESSONS

Always account for measurement error

Always account for phylogenetic uncertainty

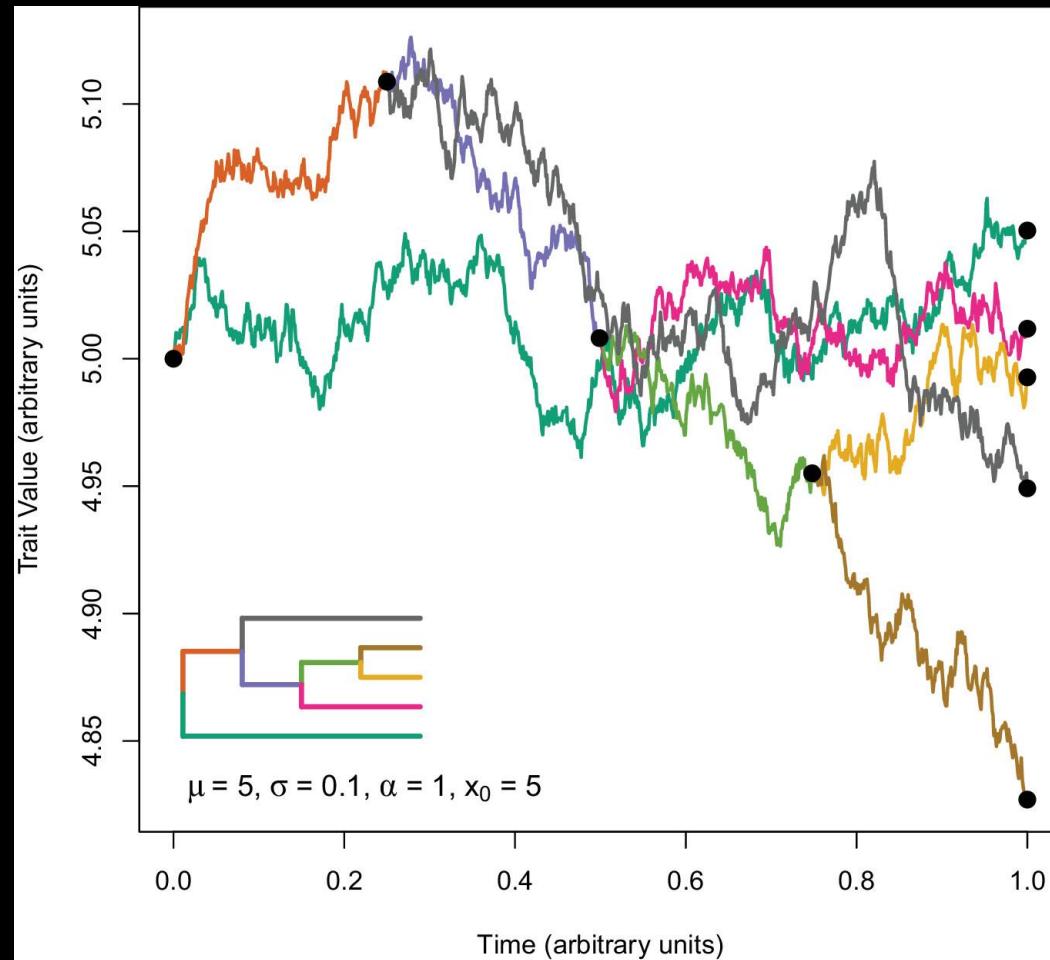
# PARAMETER ESTIMATION ERROR

Model parameters  
are estimated with  
error



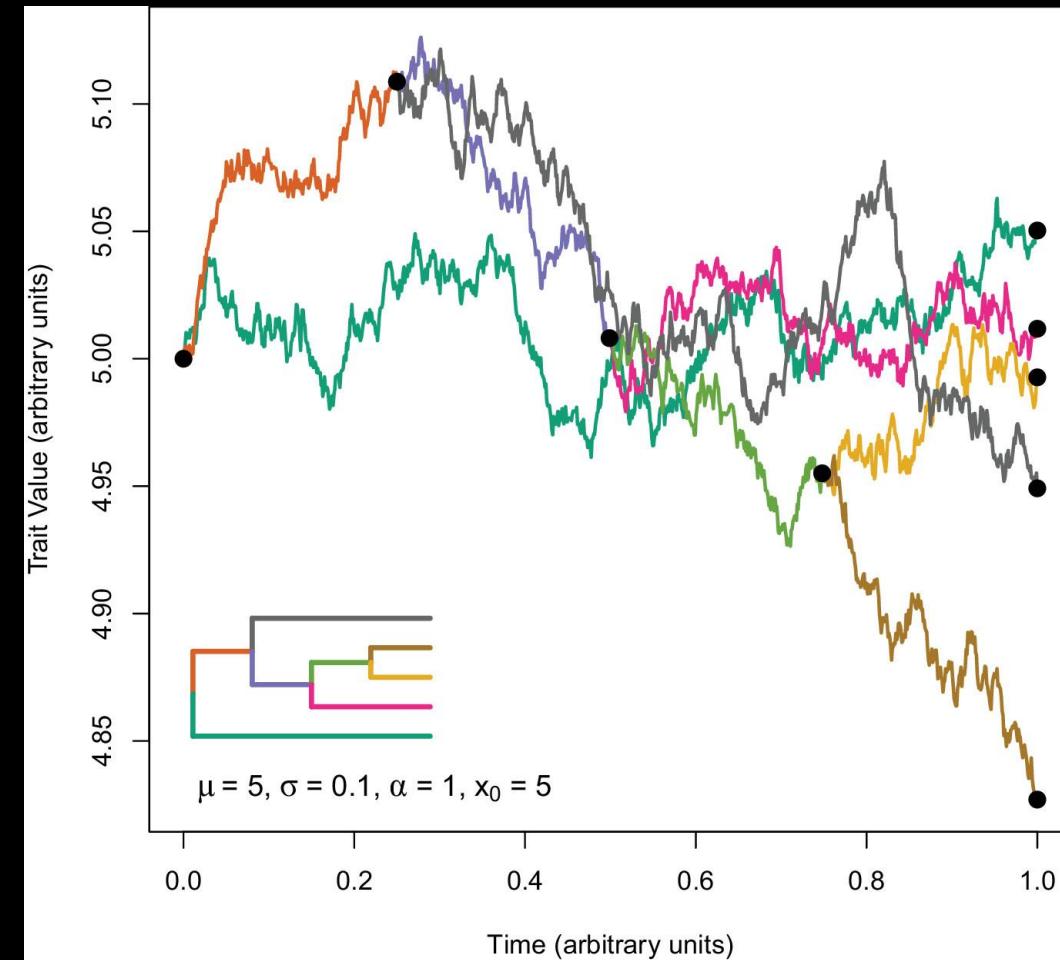
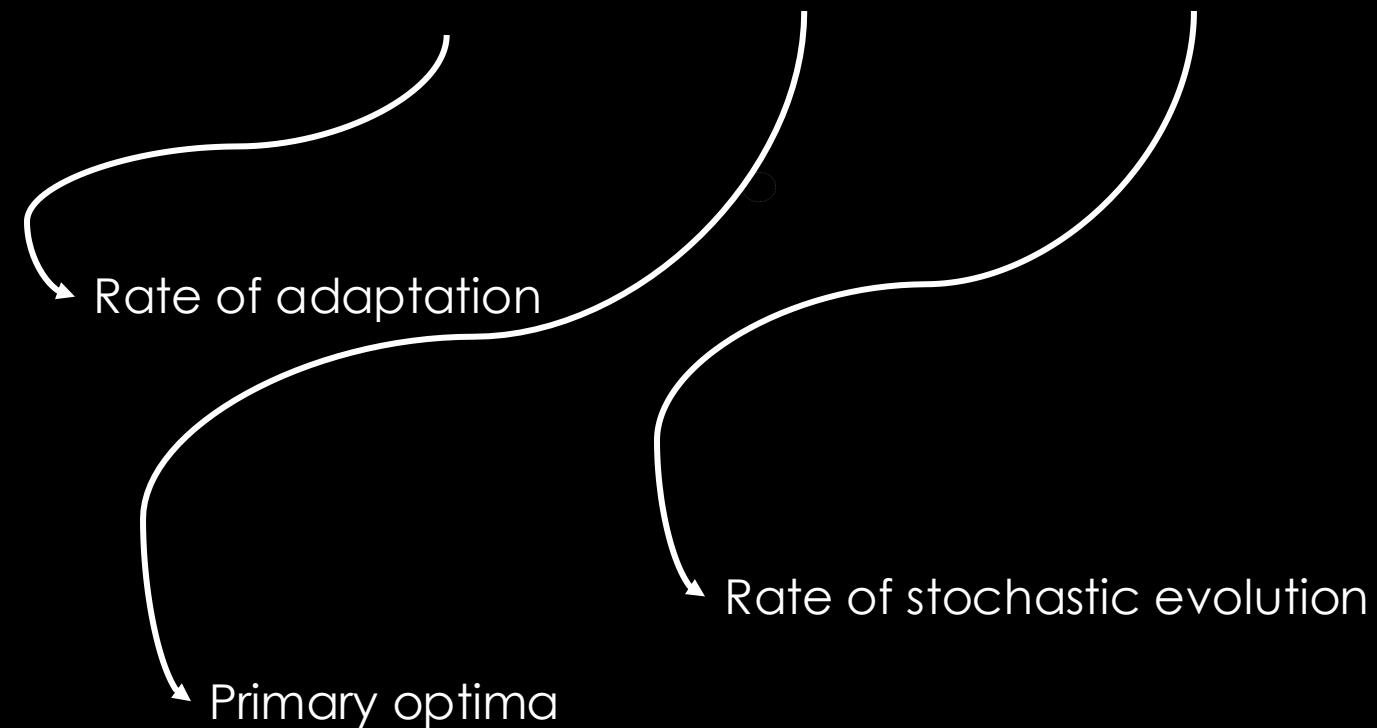
# PARAMETER ESTIMATION

$$dy = -\alpha(y(t) - \theta(t))dt + \sigma dW$$



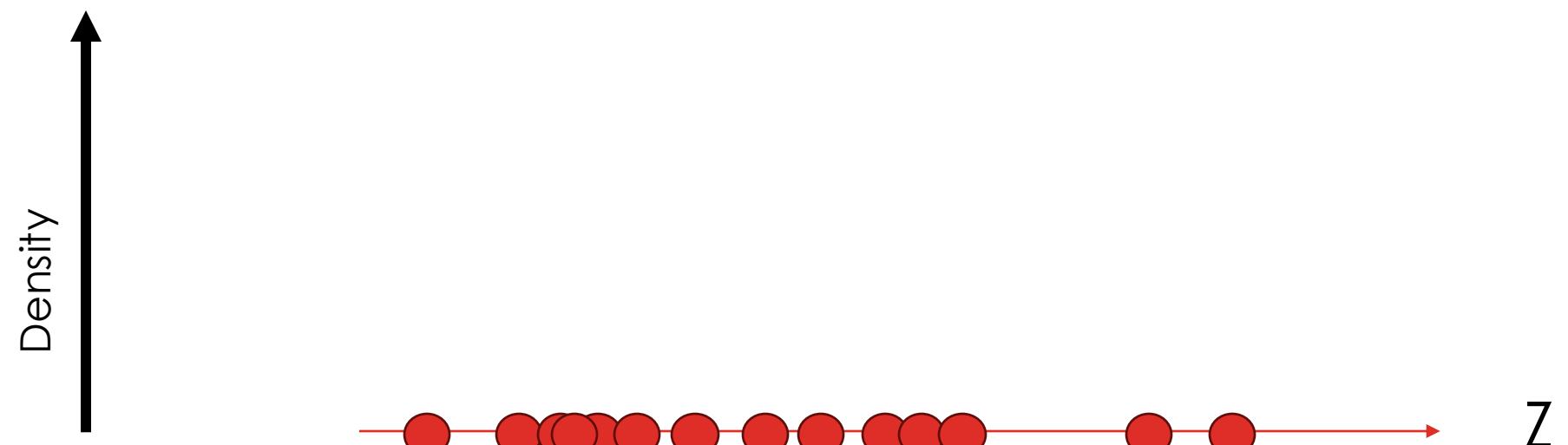
# PARAMETER ESTIMATION

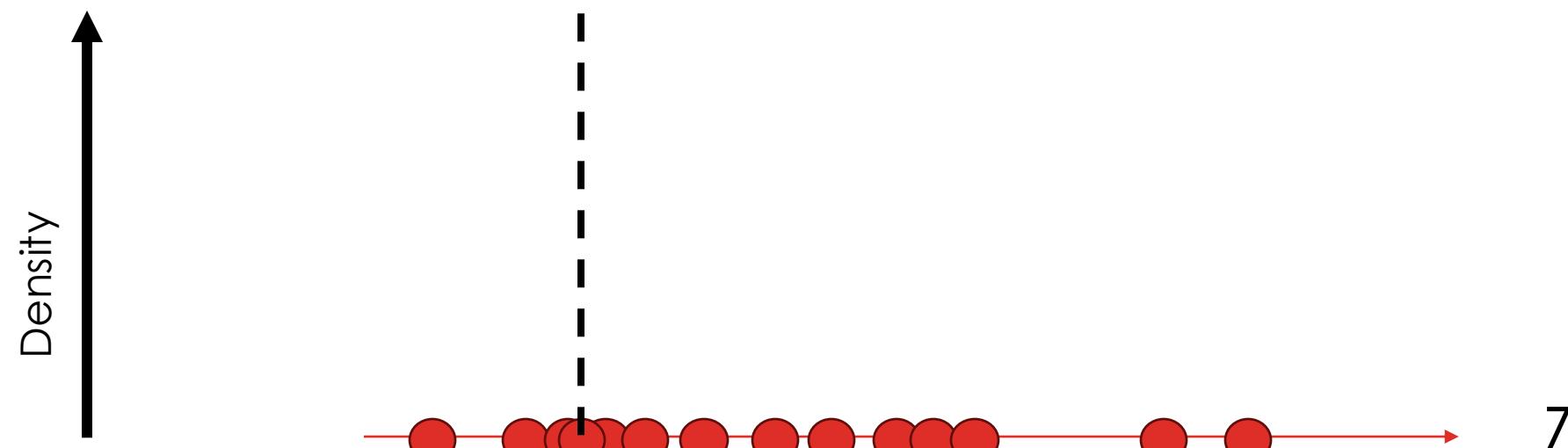
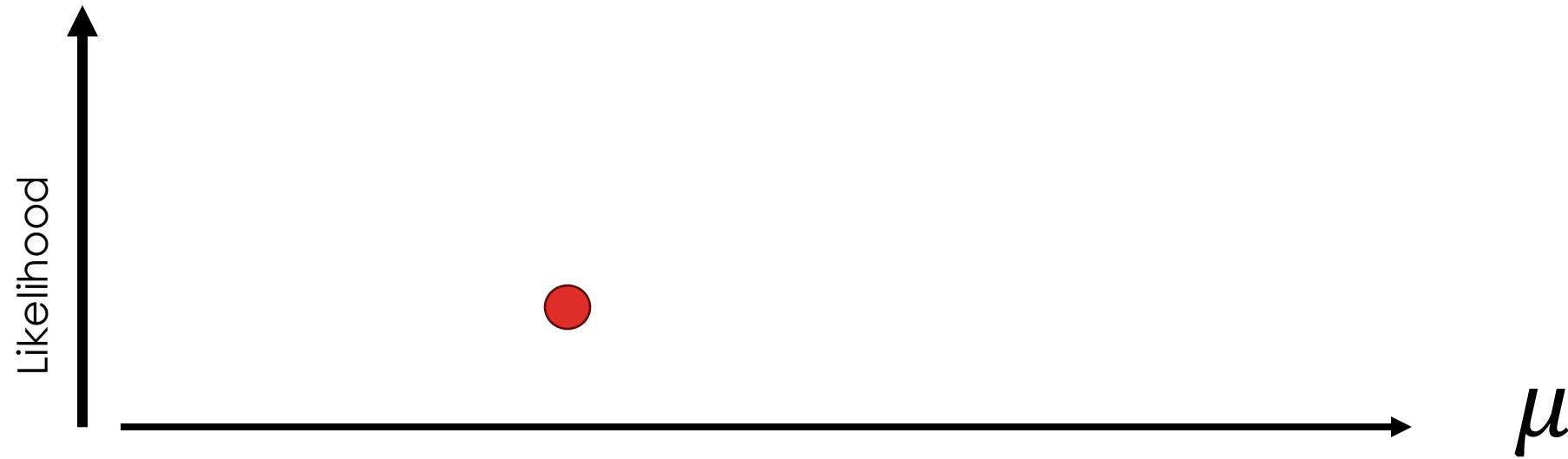
$$dy = -\alpha(y(t) - \theta(t))dt + \sigma dW$$

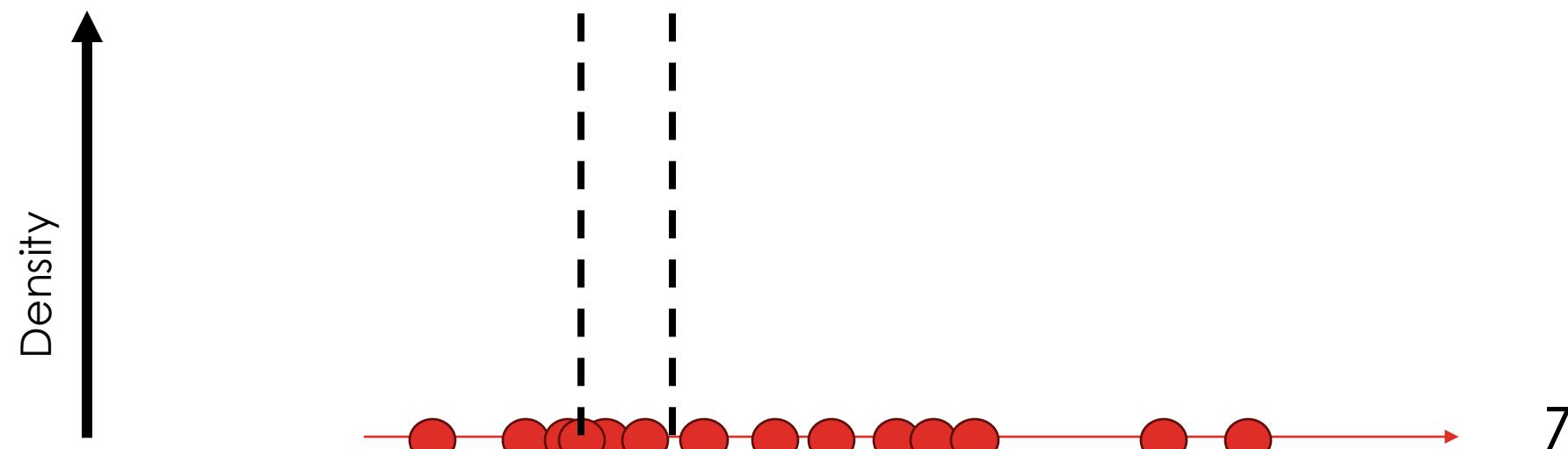
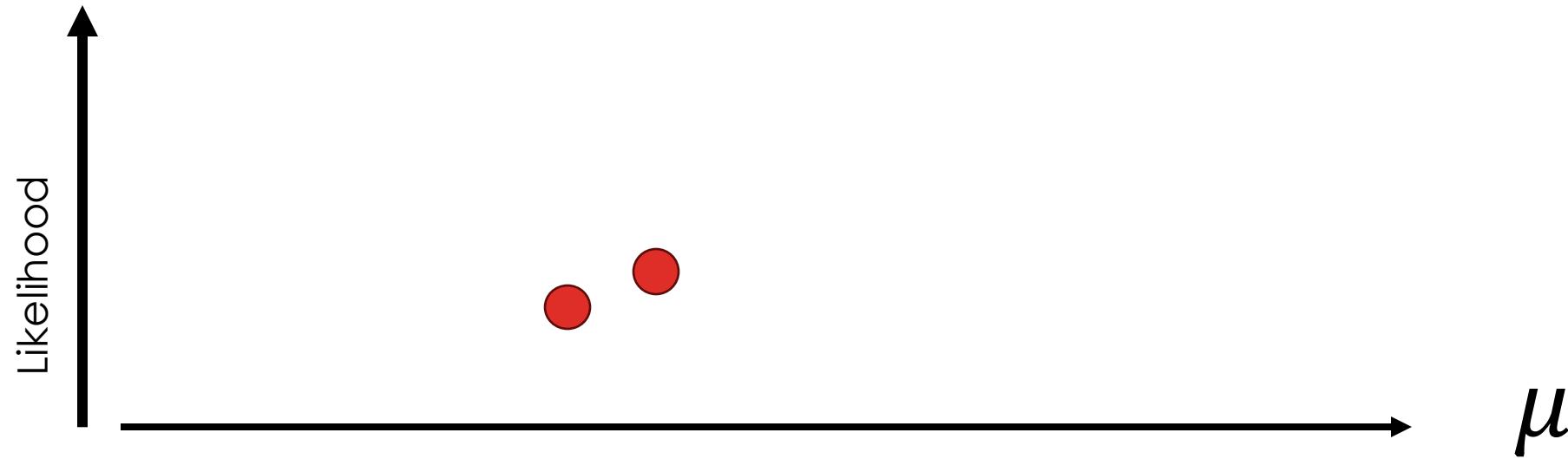


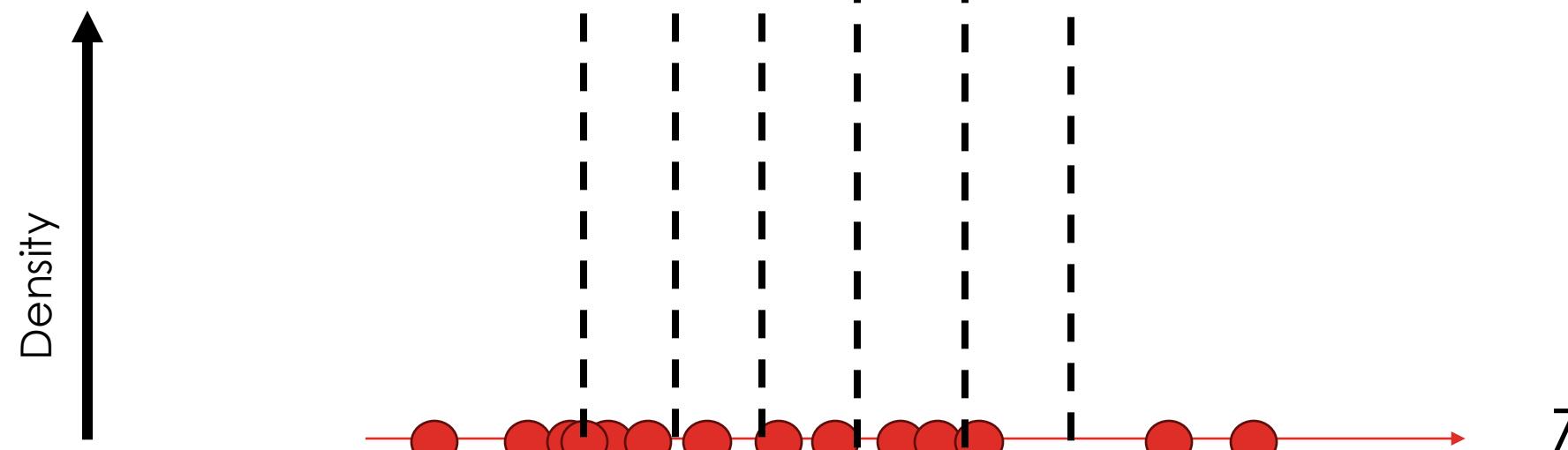
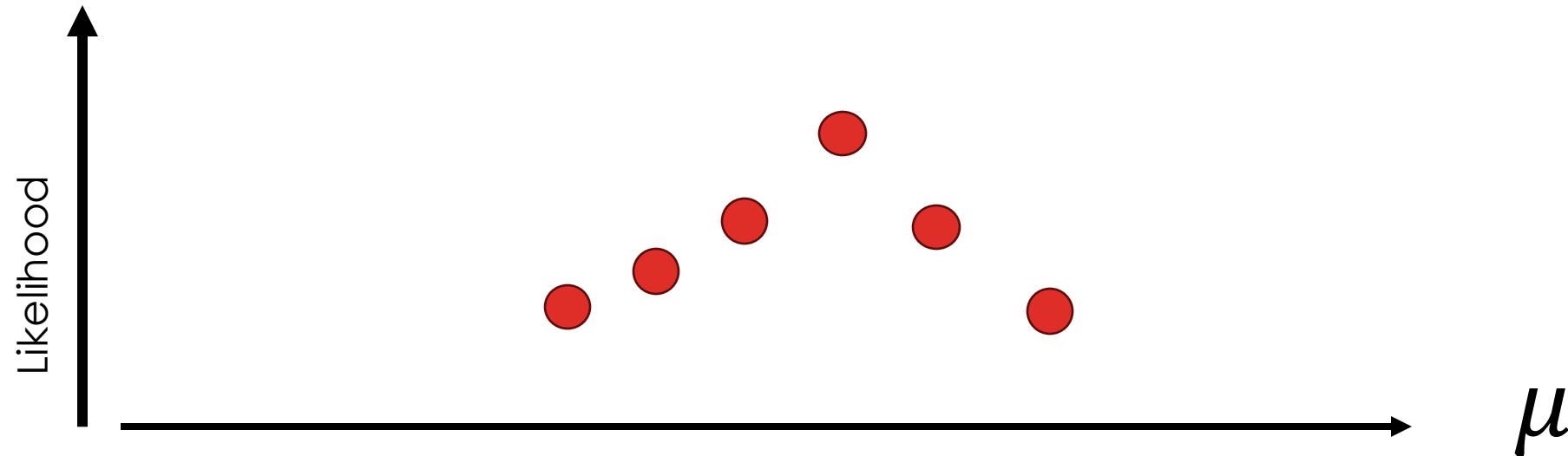
Evolutionary models have evolutionary parameters that must be estimated through data

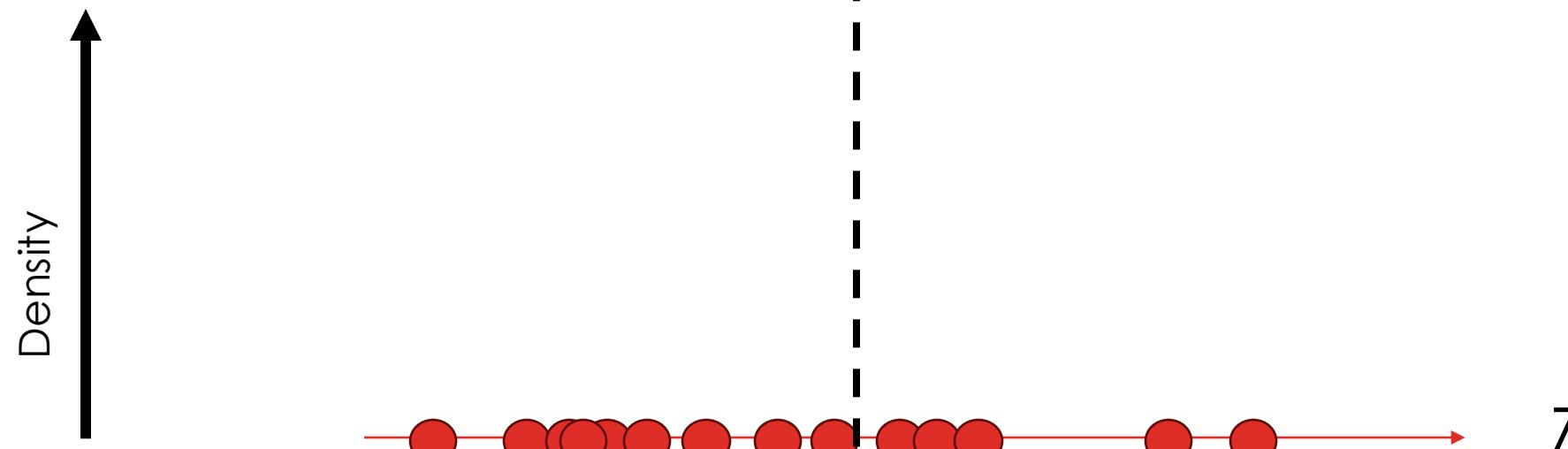
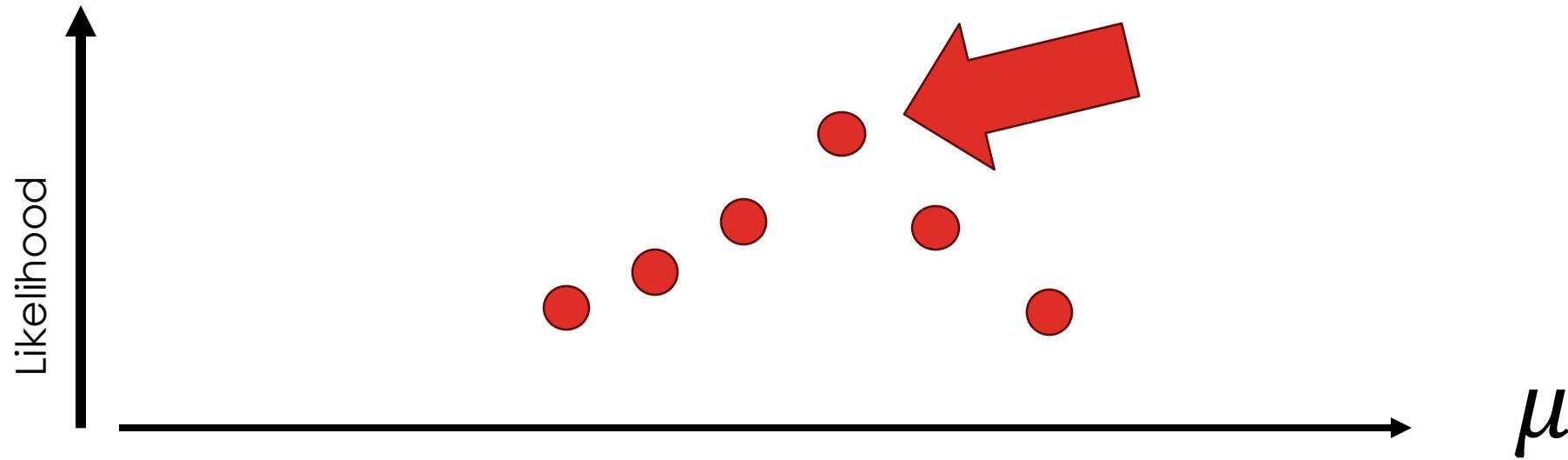
How is it done?

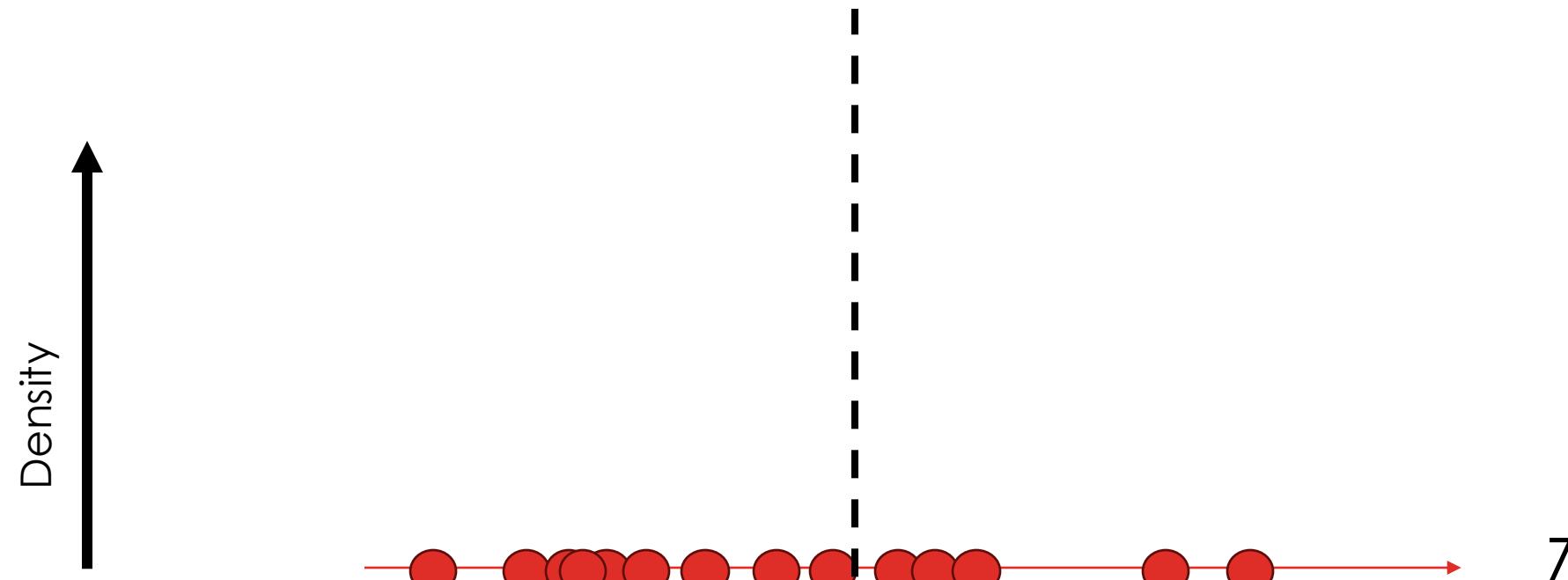
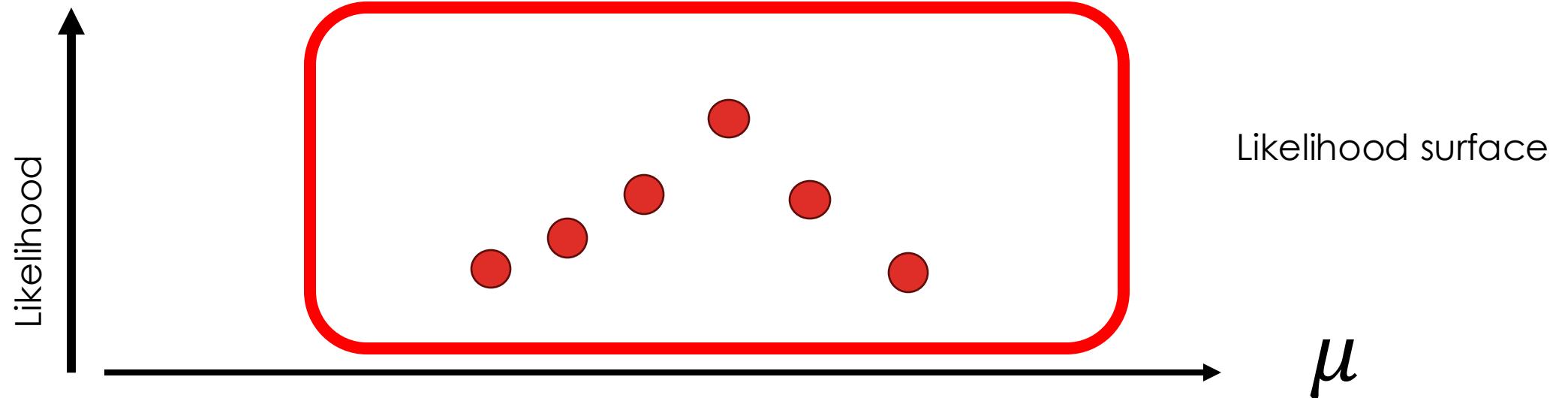


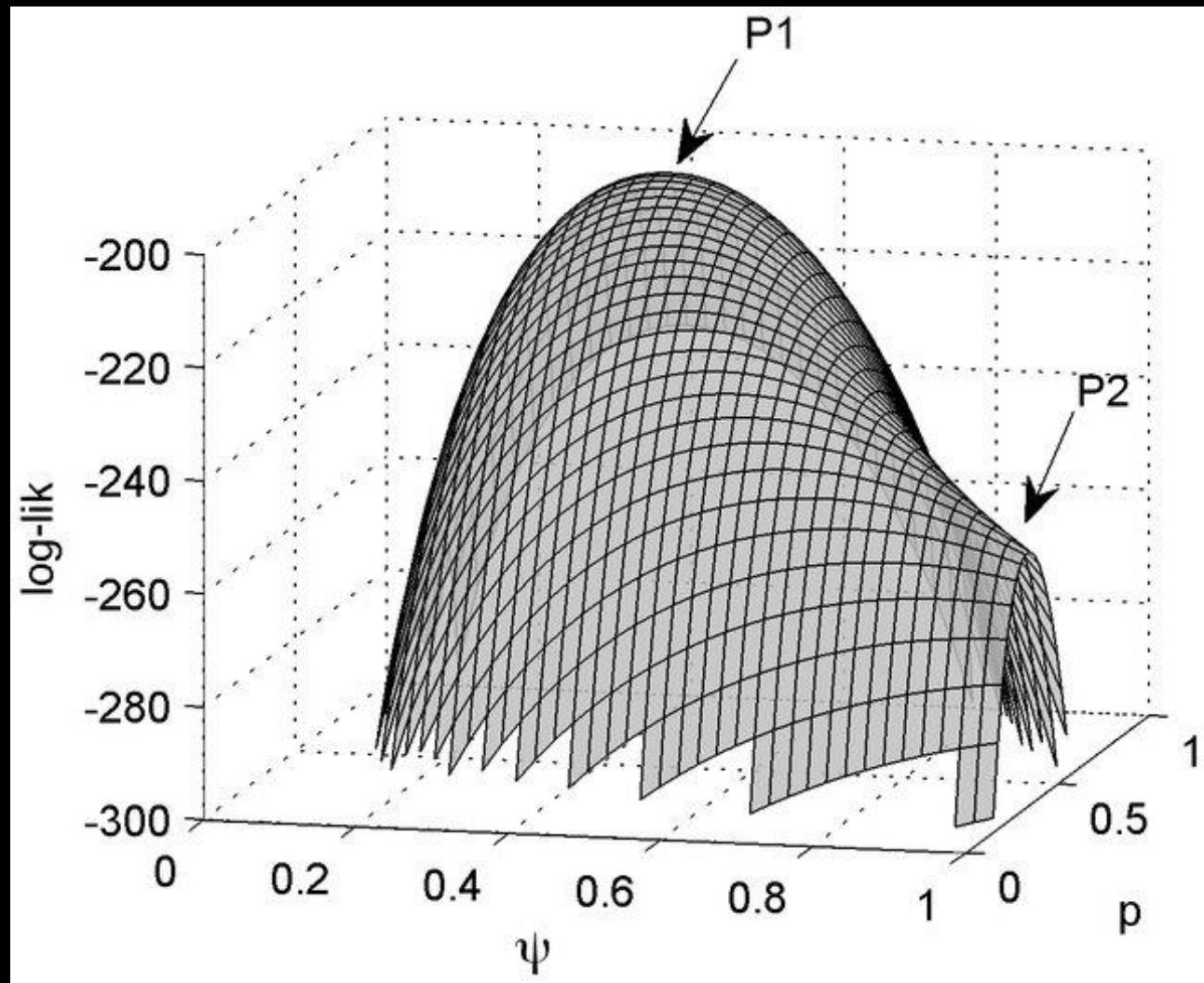




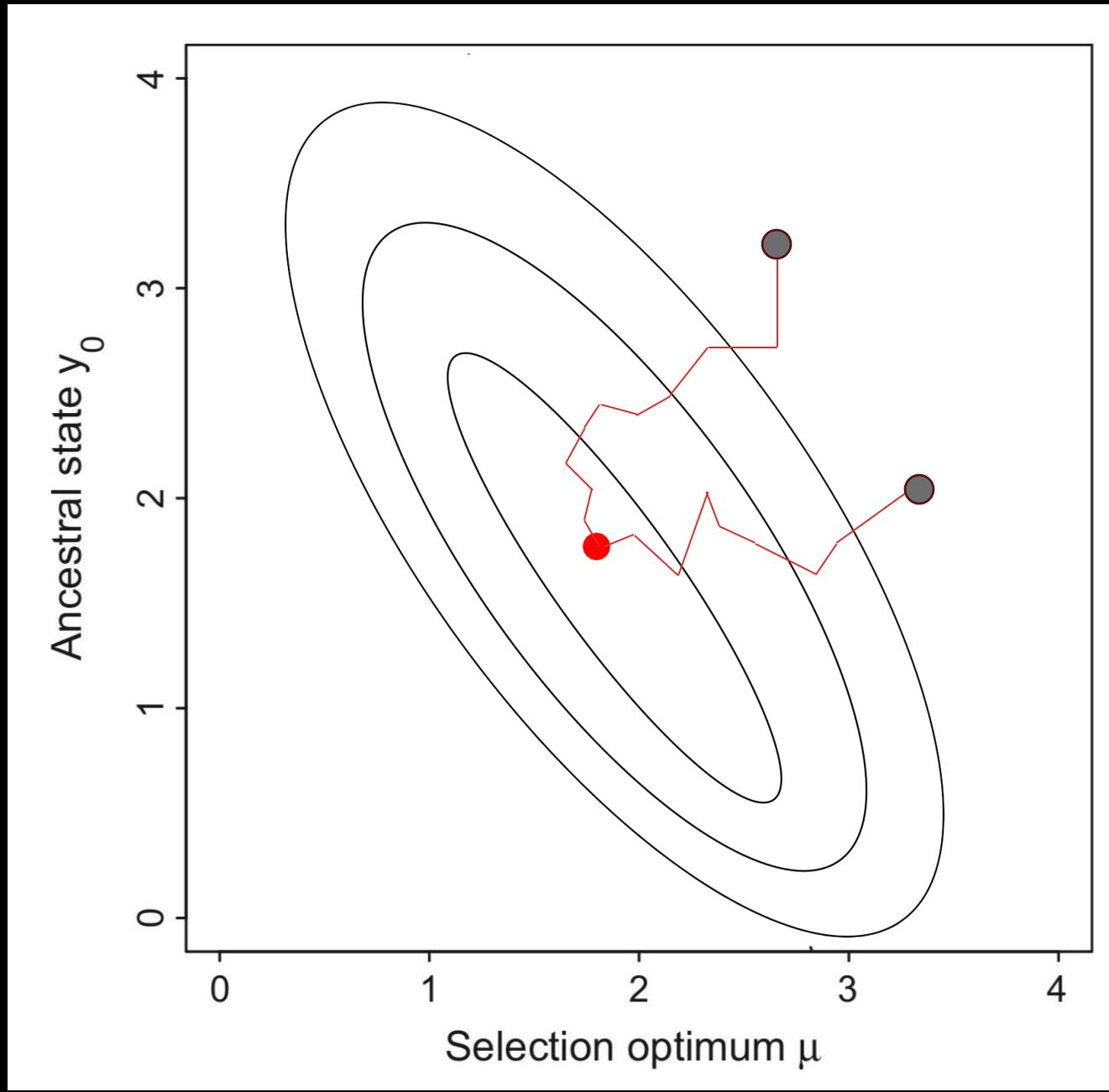




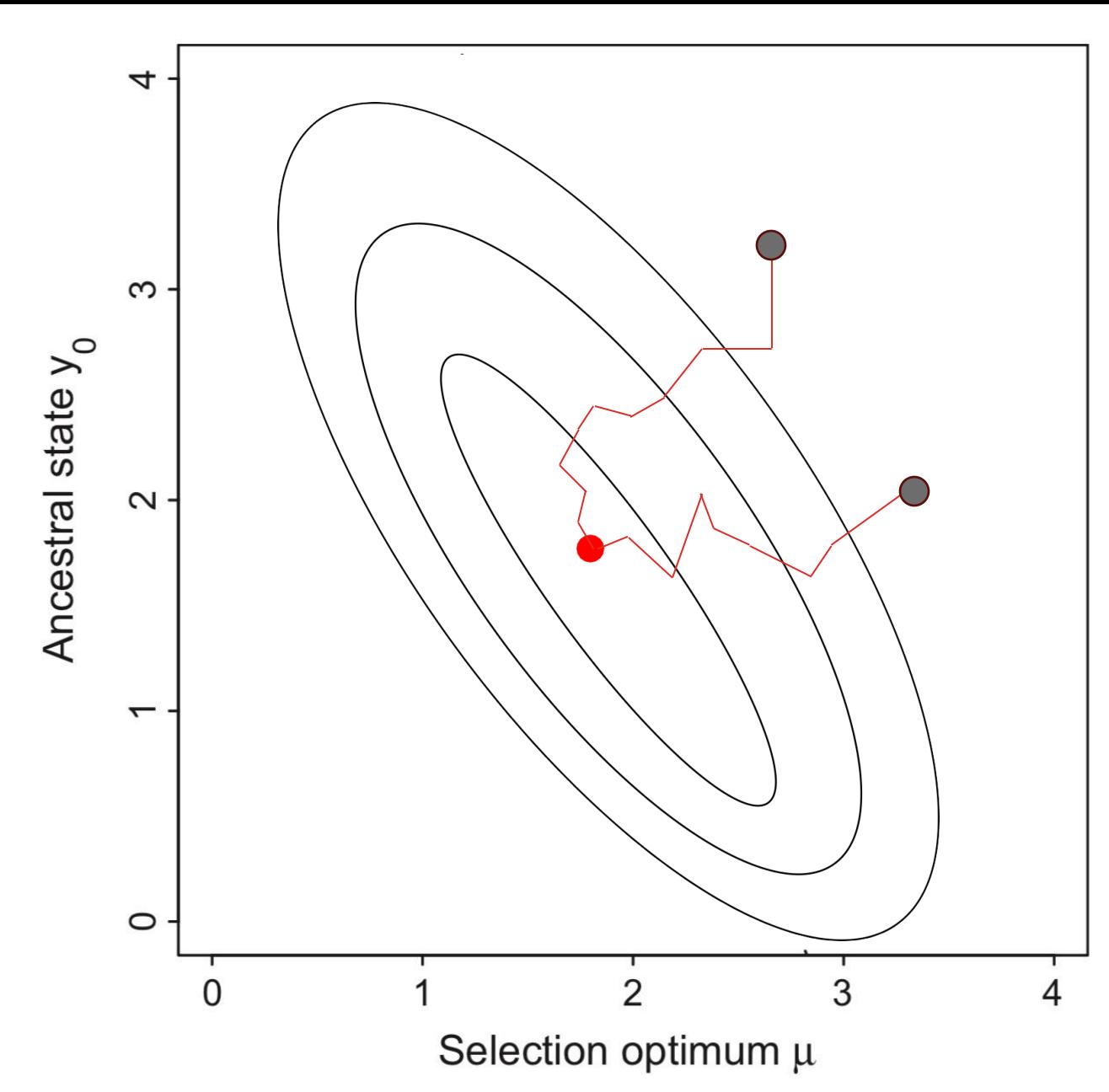




Parameter estimation is an optimization procedure on a likelihood surface

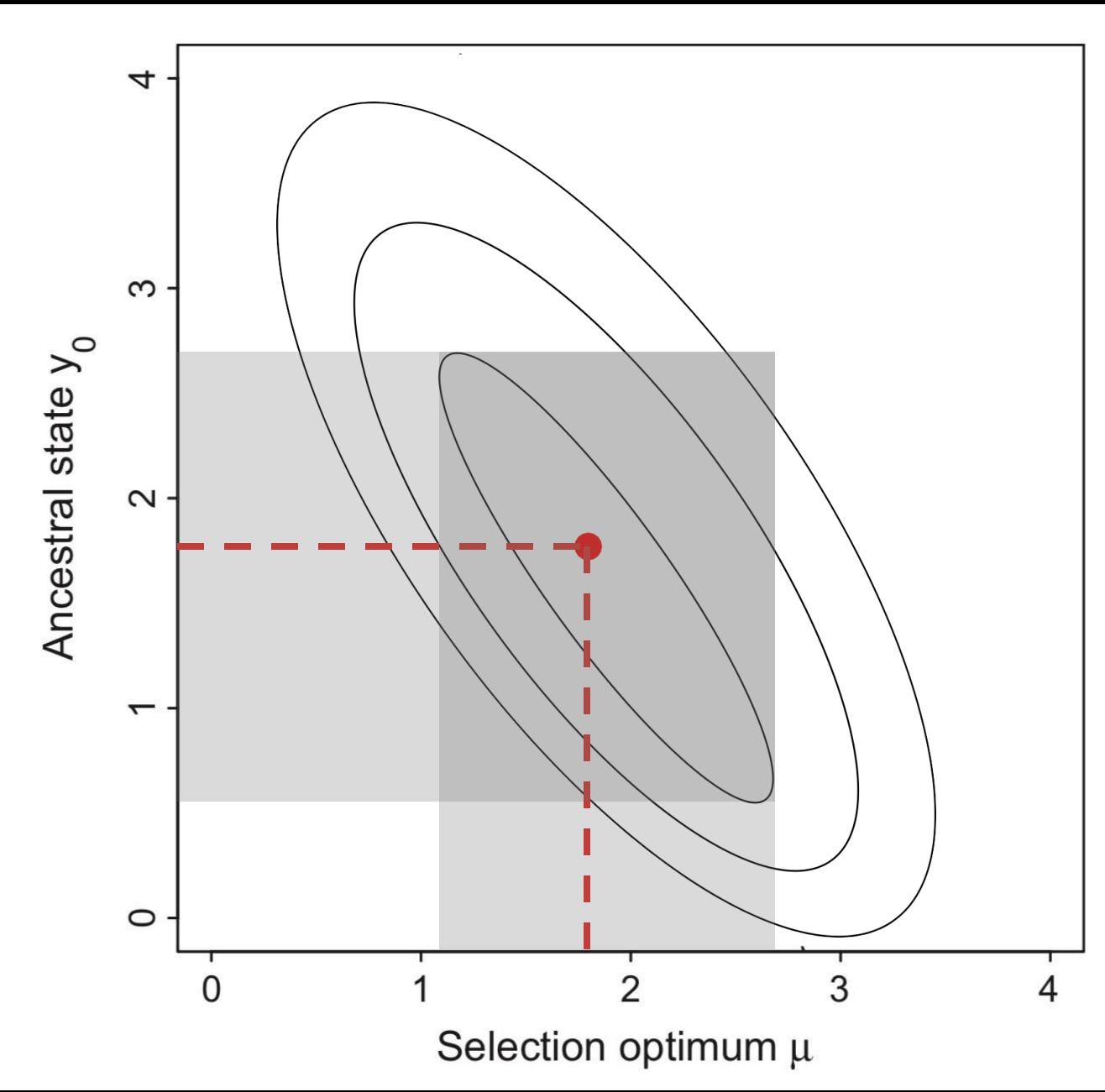


Parameter estimation is an optimization procedure on a likelihood surface



Sub-optimal likelihoods might also be considered “good enough”, specifically 2 log-lik units away from the peak

Parameter estimation is an optimization procedure on a likelihood surface

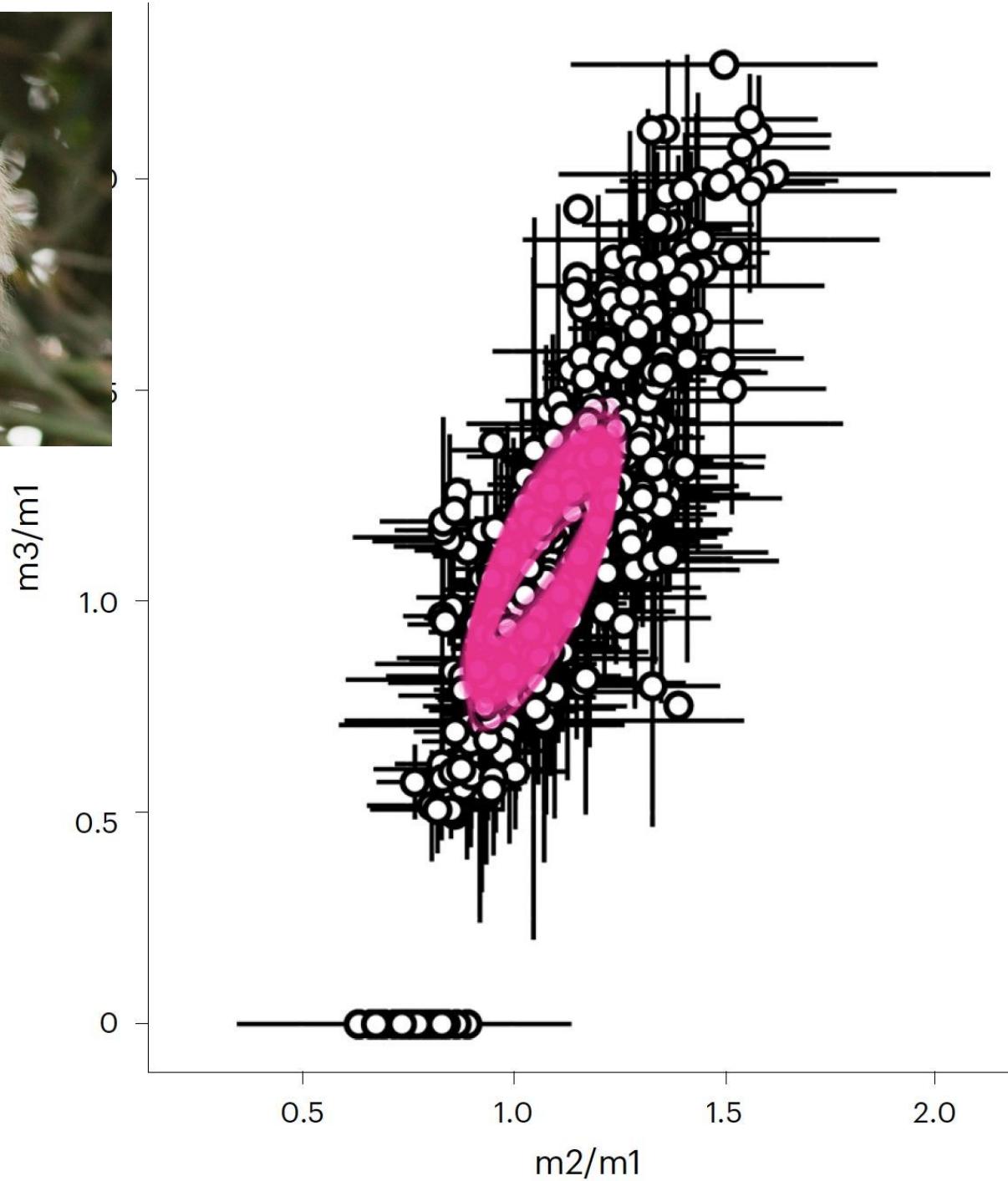


Sub-optimal likelihoods might also be considered “good enough”, specifically 2 log-lik units away from the peak

Parameter estimation is an optimization procedure on a likelihood surface



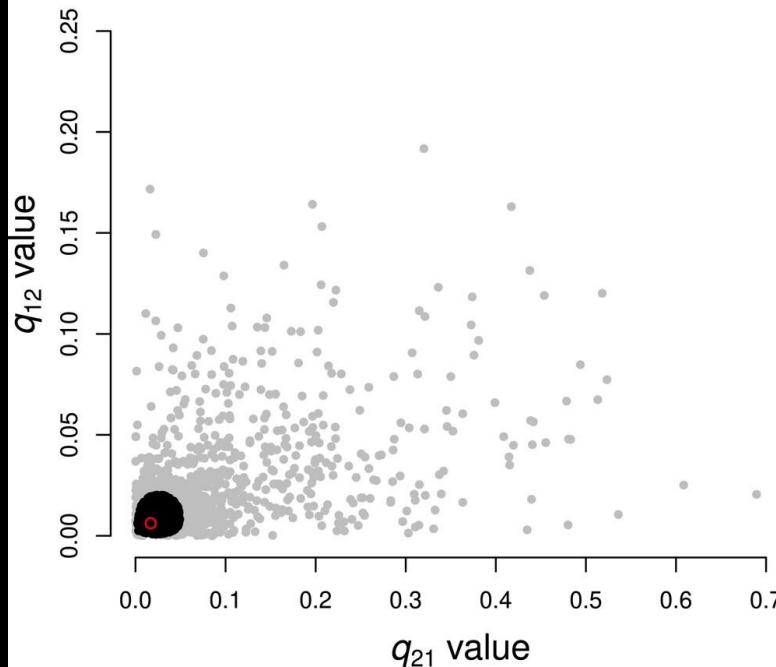
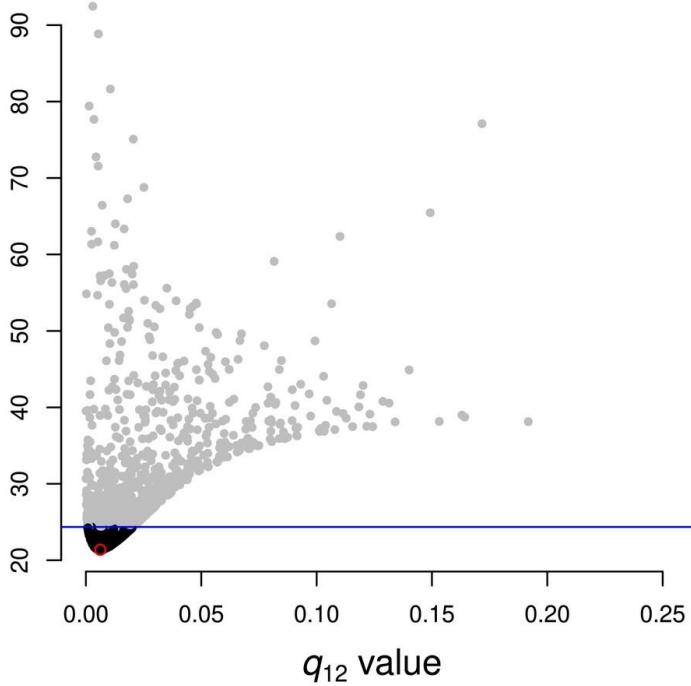
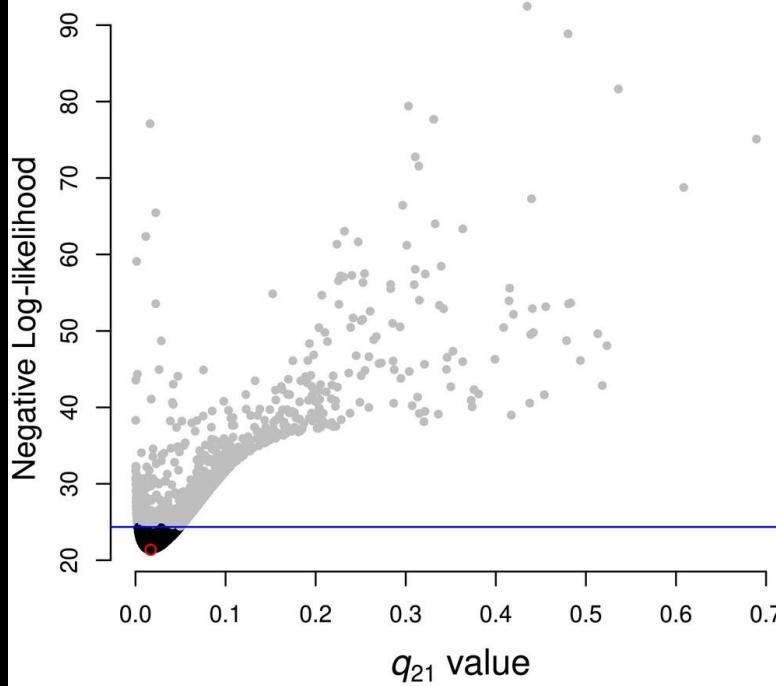
Machado et al. 2023



Rate matrix error

Can be done by  
exploring the  
likelihood surface





Dentist R package

“Dents” the likelihood  
surface for a fast  
exploration of parameter  
space

# LESSONS

Always account for measurement error

Always account for phylogenetic uncertainty

Always account for parameter estimation error

# MODEL ADEQUACY

Sometimes the best model  
is not the best model

The Far Side / BY GARY LARSON



Donning his new canine decoder,  
Professor Schwartzman becomes the first  
human being on Earth to hear what  
barking dogs are actually saying.

## interpretation



Models



inadequacy

“Estimated data”  
(phylogenies)



error/  
inadequacy

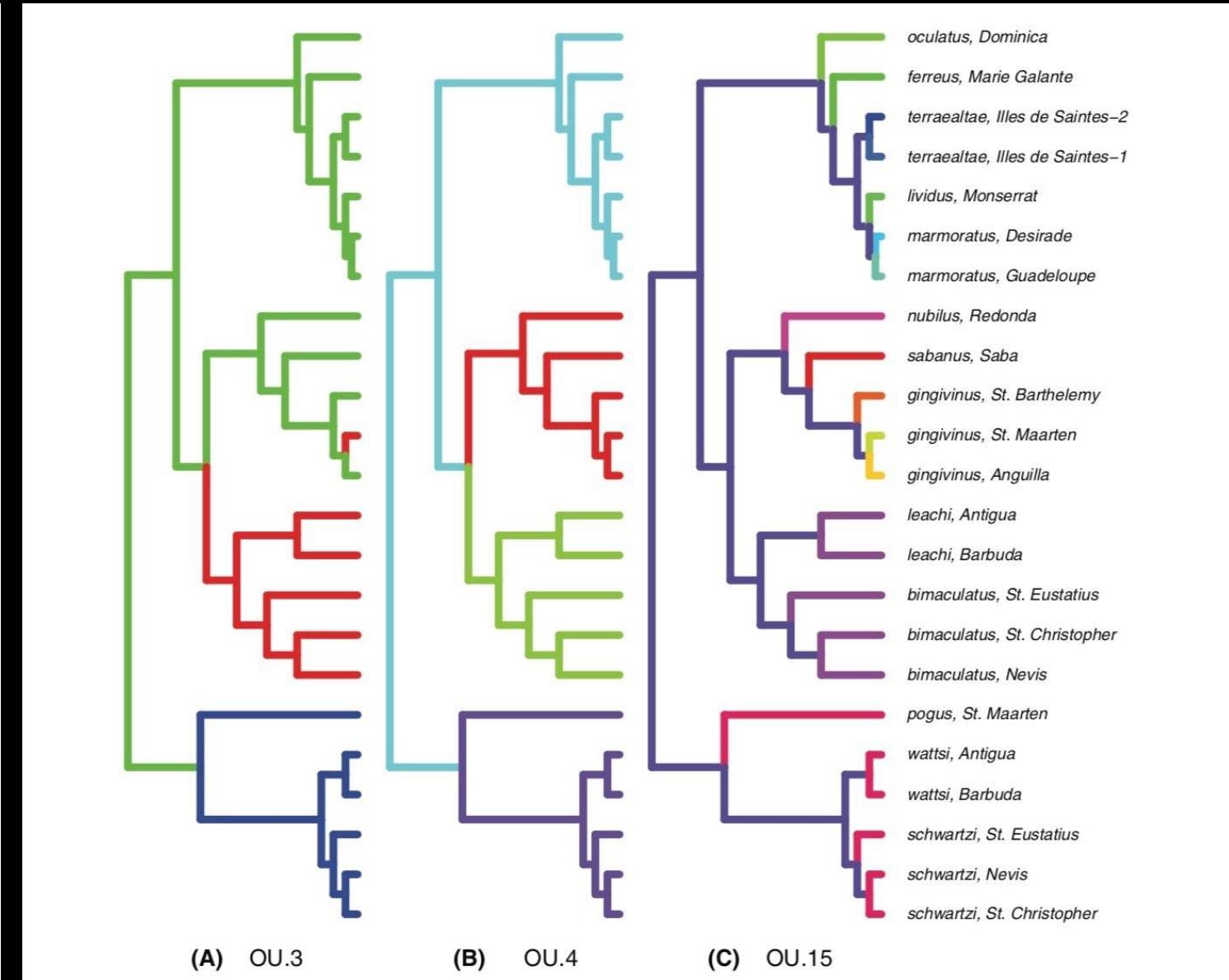
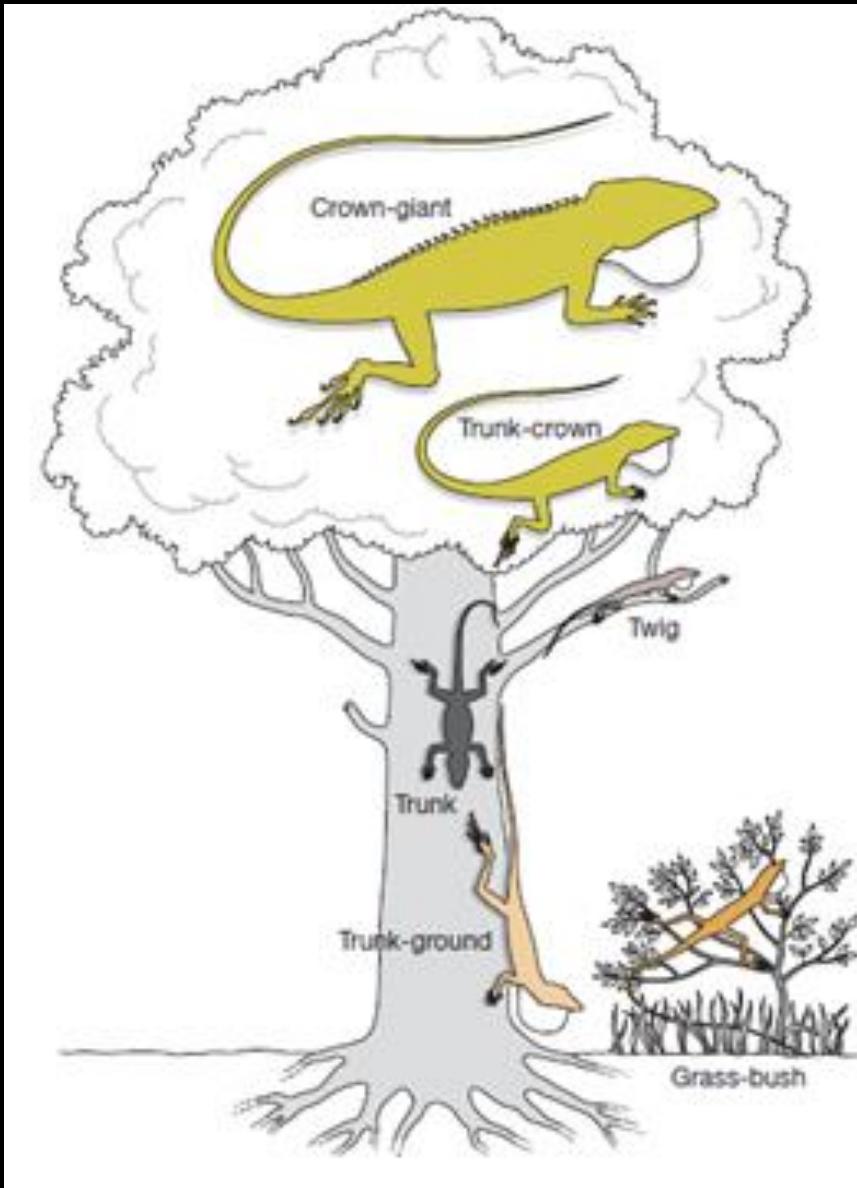
Data



error

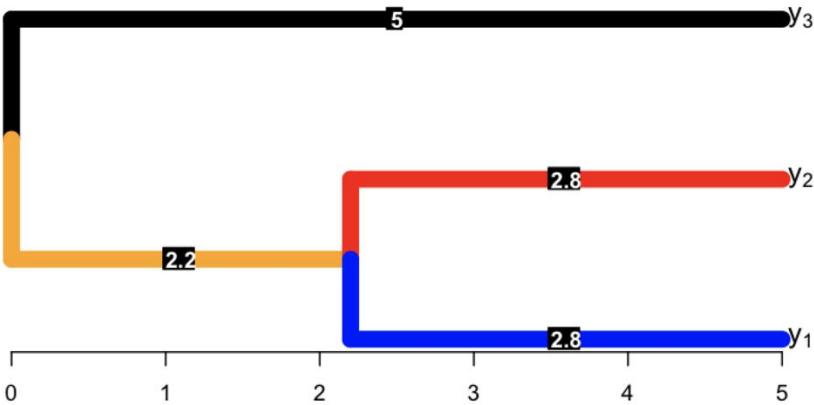
It's possible for the  
best model is not the  
best

# Adaptive radiation of Anoles

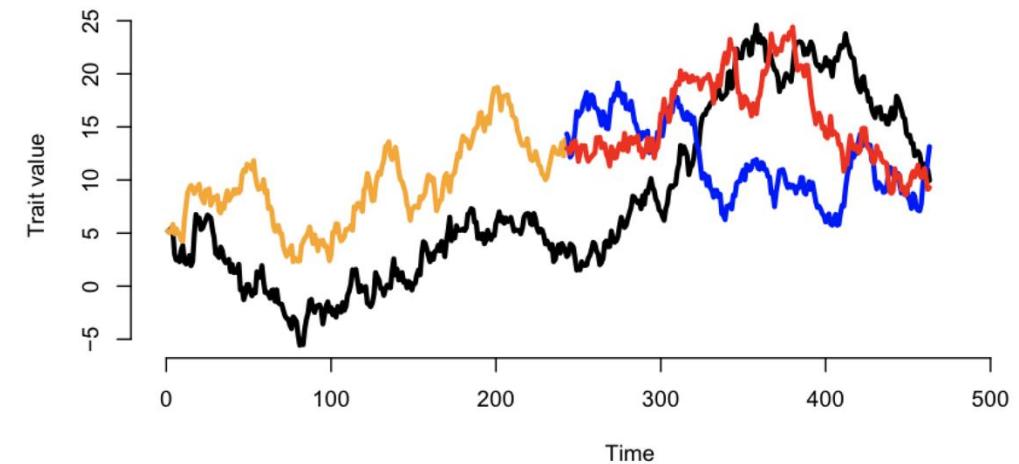


“Best models” (<2 loglik of best)

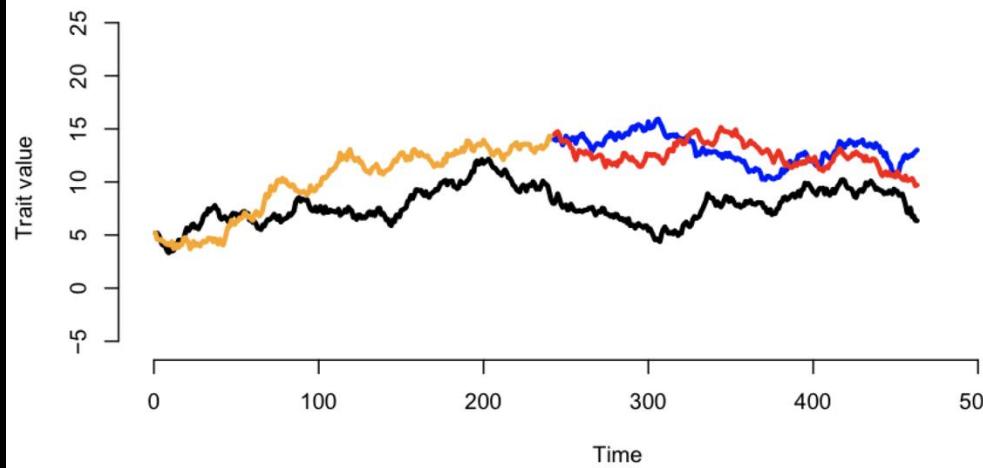
Phylogenetic Tree of 3 Taxa



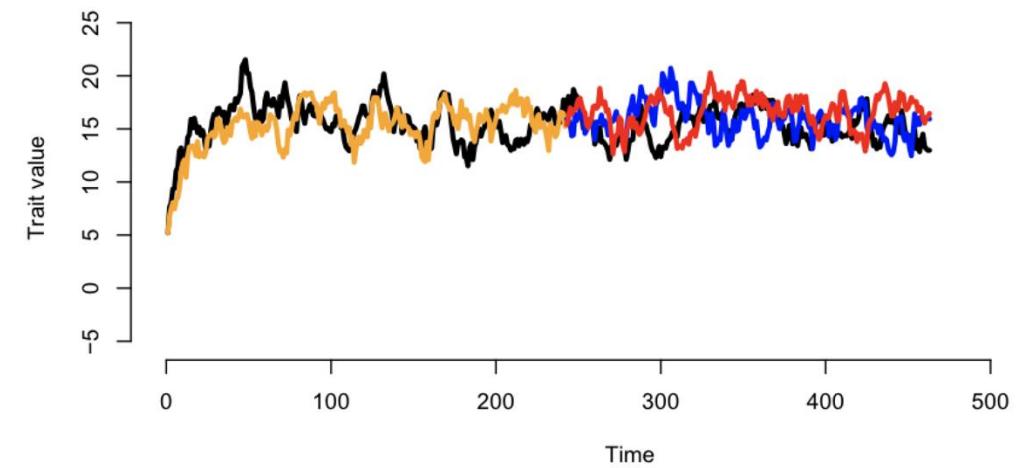
$$\text{BM: } y_{it} = \sigma dW_t$$



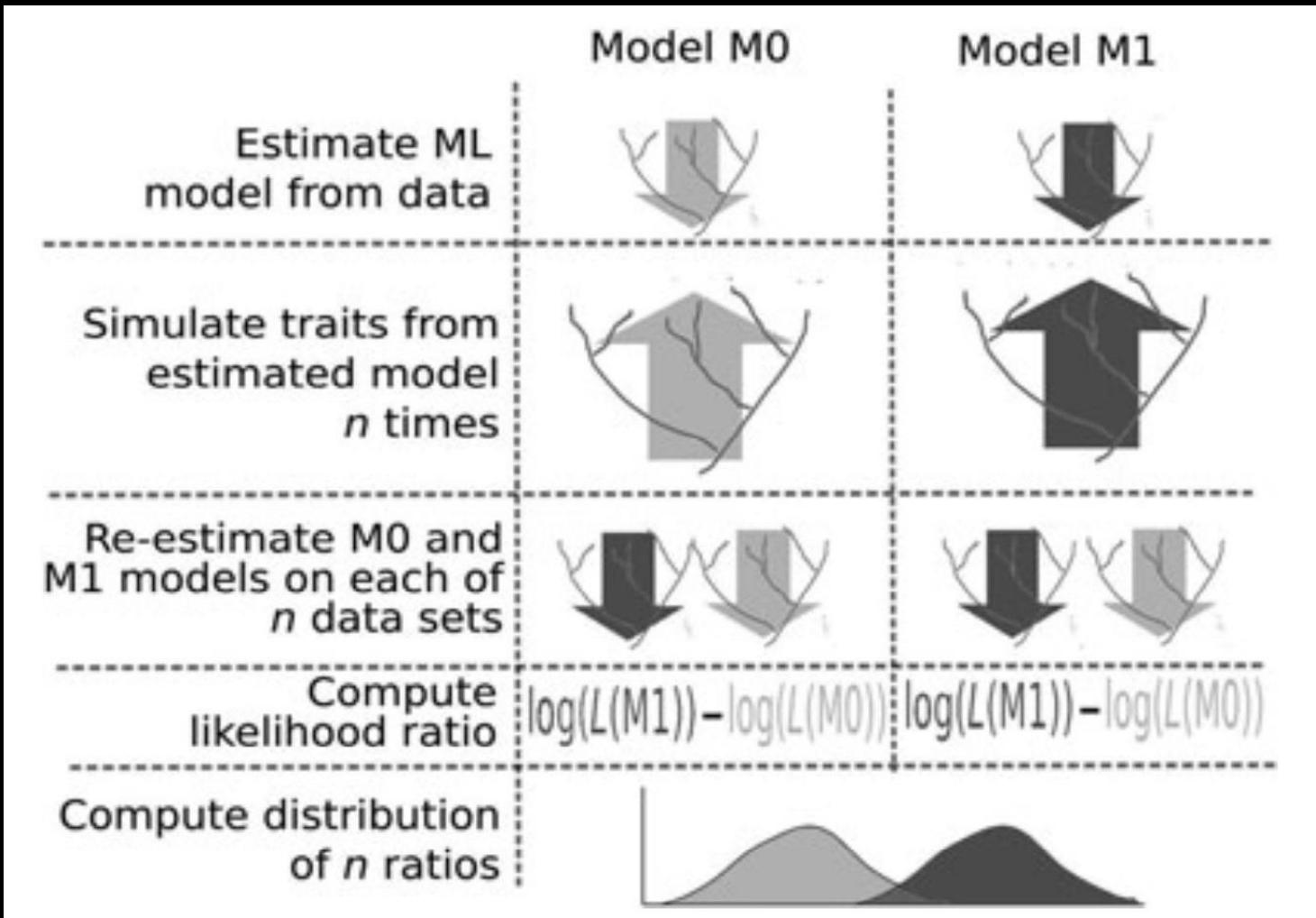
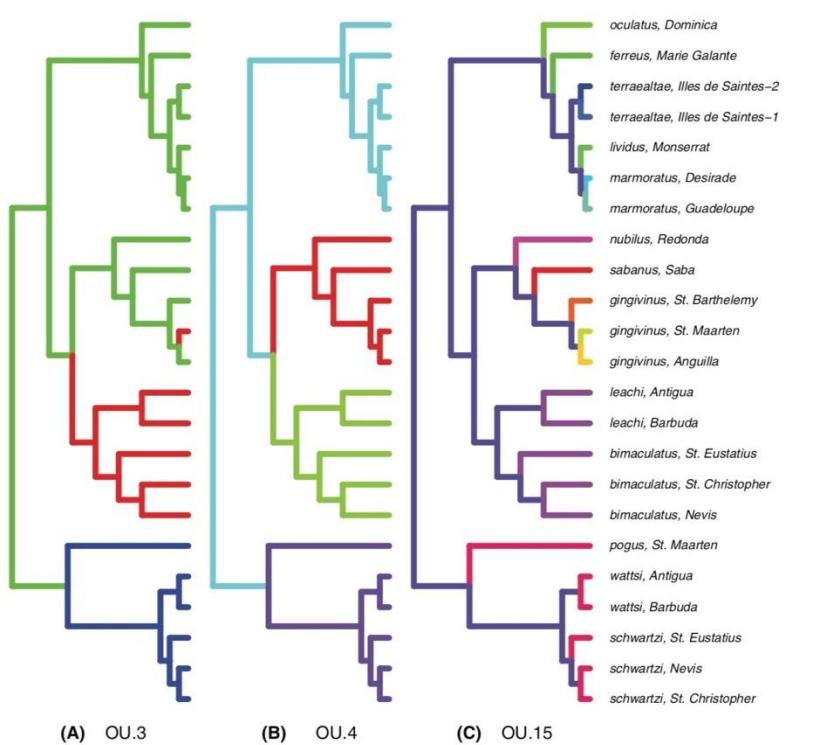
$$\text{EB: } y_{it} = \sigma e^{rt} dW_t$$



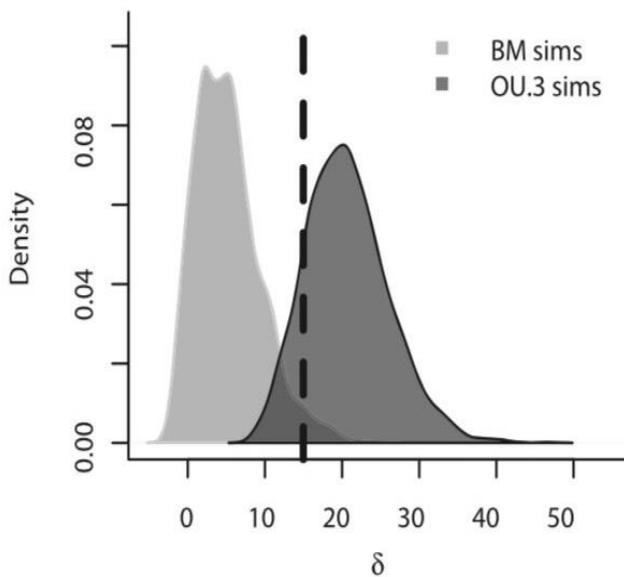
$$\text{OU: } y_{it} = \alpha(\theta - y_{it})dt + \sigma dW_t$$



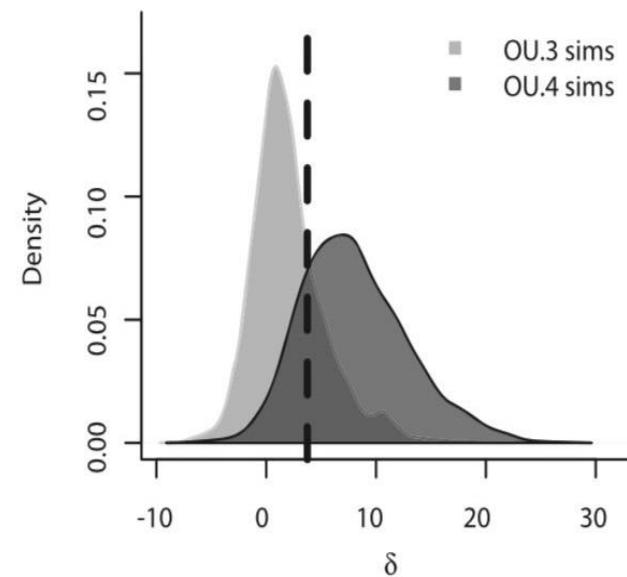
Simulations might help us understand our data



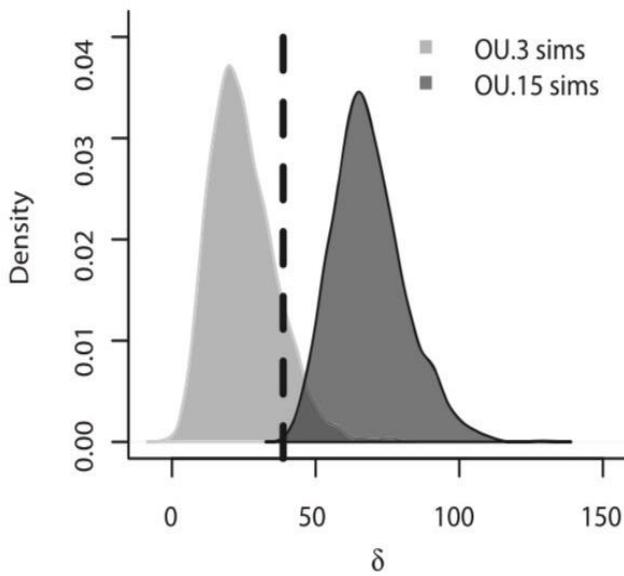
(A) BM vs. OU.3



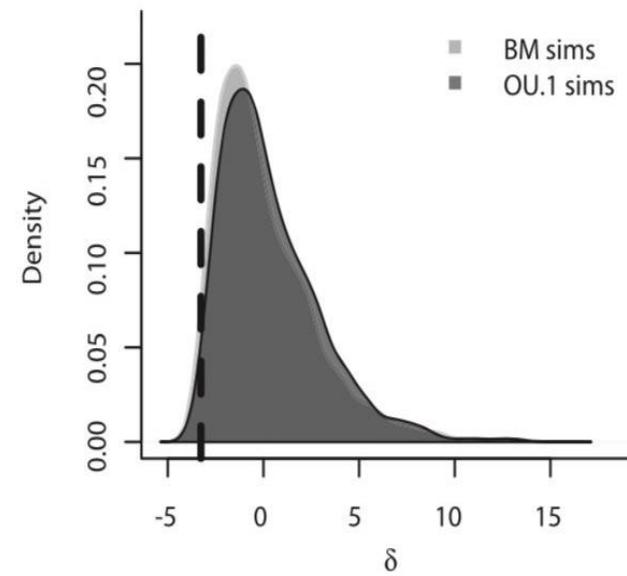
(B) OU.3 vs. OU.4



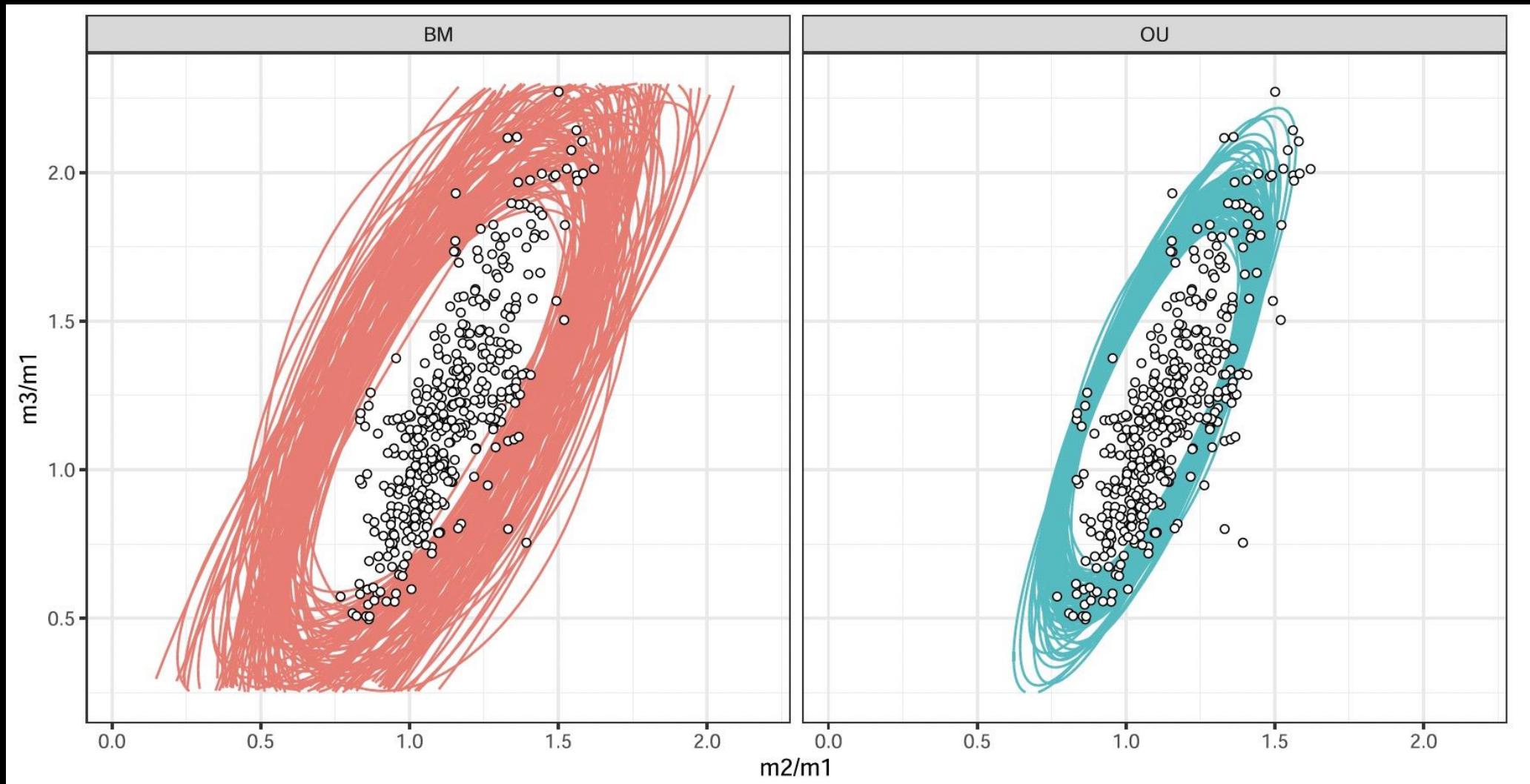
(C) OU.3 vs. OU.15



(D) BM vs. OU.1

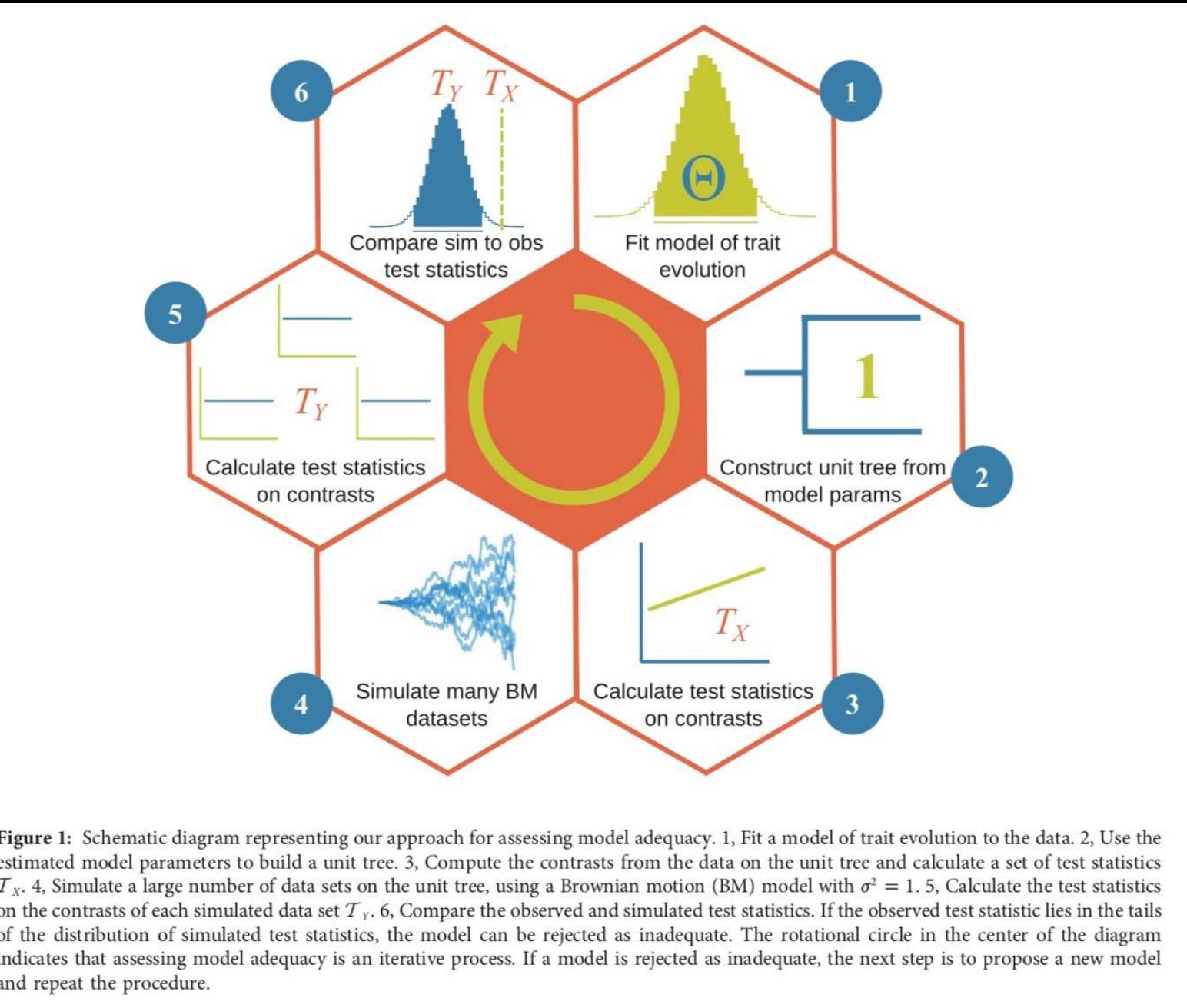


## Visual inspection

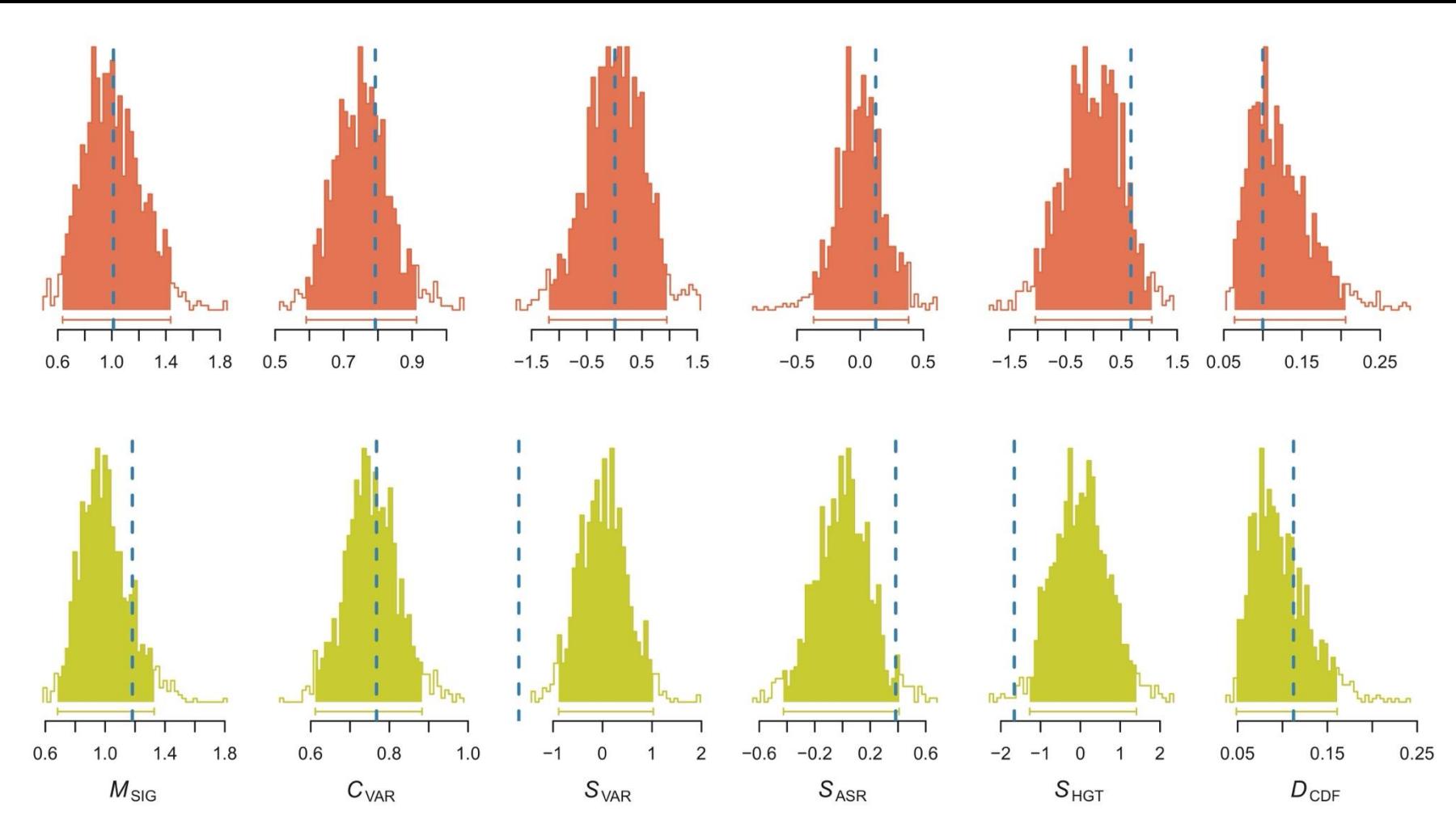


Bad models will generate data  
that does not match empirical  
observations

Machado et al. 2023



**Figure 1:** Schematic diagram representing our approach for assessing model adequacy. 1, Fit a model of trait evolution to the data. 2, Use the estimated model parameters to build a unit tree. 3, Compute the contrasts from the data on the unit tree and calculate a set of test statistics  $T_X$ . 4, Simulate a large number of data sets on the unit tree, using a Brownian motion (BM) model with  $\sigma^2 = 1.5$ . 5, Calculate the test statistics on the contrasts of each simulated data set  $T_Y$ . 6, Compare the observed and simulated test statistics. If the observed test statistic lies in the tails of the distribution of simulated test statistics, the model can be rejected as inadequate. The rotational circle in the center of the diagram indicates that assessing model adequacy is an iterative process. If a model is rejected as inadequate, the next step is to propose a new model and repeat the procedure.



**Figure 2:** Illustration of our approach to model adequacy. We fitted three models (Brownian motion, Ornstein-Uhlenbeck [OU], and early burst) to seed mass data from two different tree families, the Meliaceae (top, red) and the Fagaceae (bottom, yellow). In both cases, an OU model (analyzed here) was strongly supported when fitted with maximum likelihood. The plotted distributions are the test statistics ( $M_{\text{SIG}}$ ,  $C_{\text{VAR}}$ ,  $S_{\text{VAR}}$ ,  $S_{\text{ASR}}$ ,  $S_{\text{HGT}}$ ,  $D_{\text{CDF}}$ ) calculated from the contrasts of the simulated data; the bars underneath the plots represent 95% of the density. The dashed vertical lines are the values of the test statistics calculated on the contrasts of the observed data. Using our test statistics, an OU model appears to be an adequate model for the evolution of seed mass in the Meliaceae; for all of the test statistics, the observed test statistic lies in the middle of the distribution of simulated test statistics. For the Fagaceae, the slopes of the contrasts against their expected variances  $S_{\text{VAR}}$  and node height  $S_{\text{HGT}}$  are much lower than the expectations under the model.

# LESSONS

Always account for measurement error

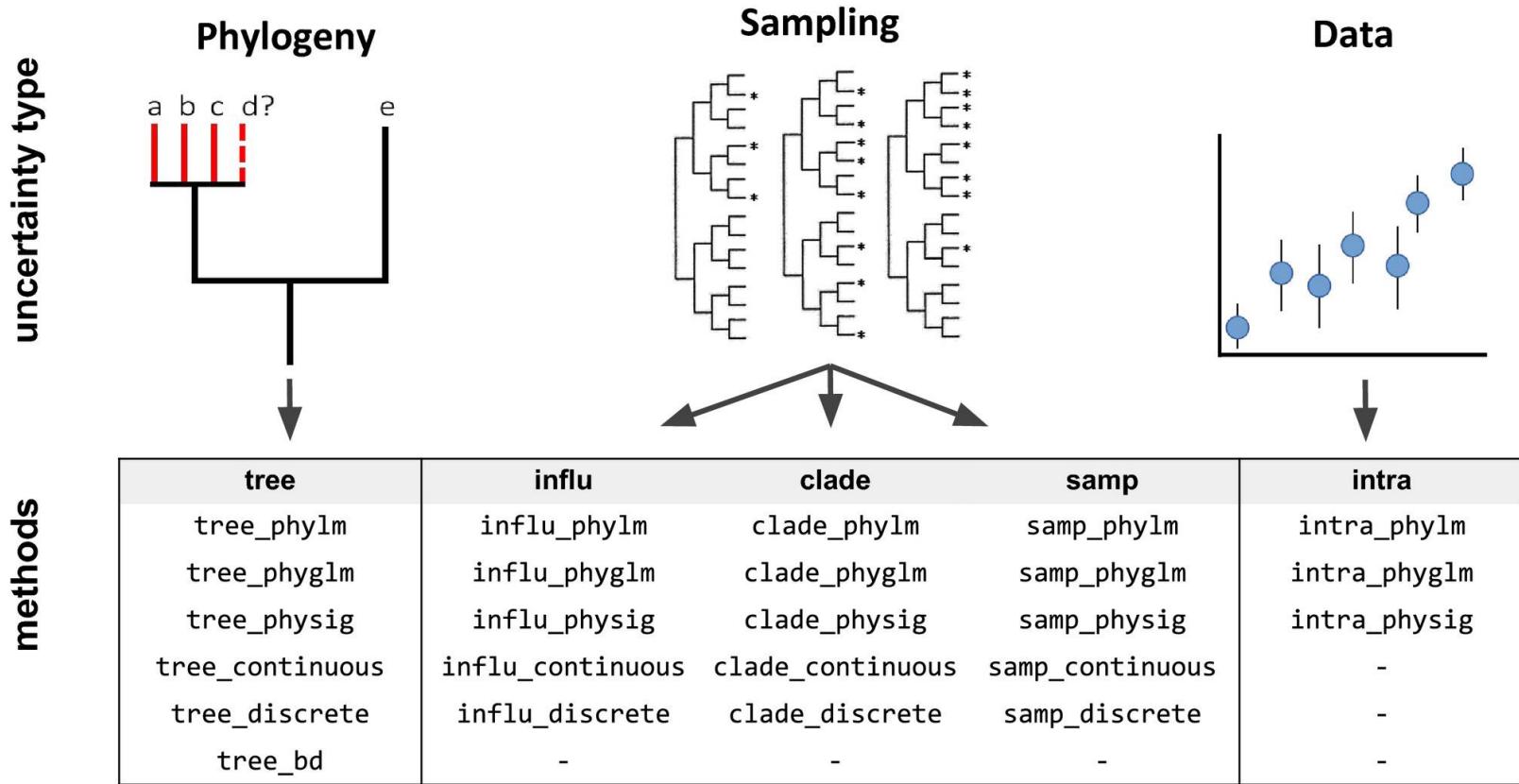
Always account for phylogenetic uncertainty

Always account for parameter estimation error

Always account for model inadequacy

# SENSITIVITY ANALYSIS

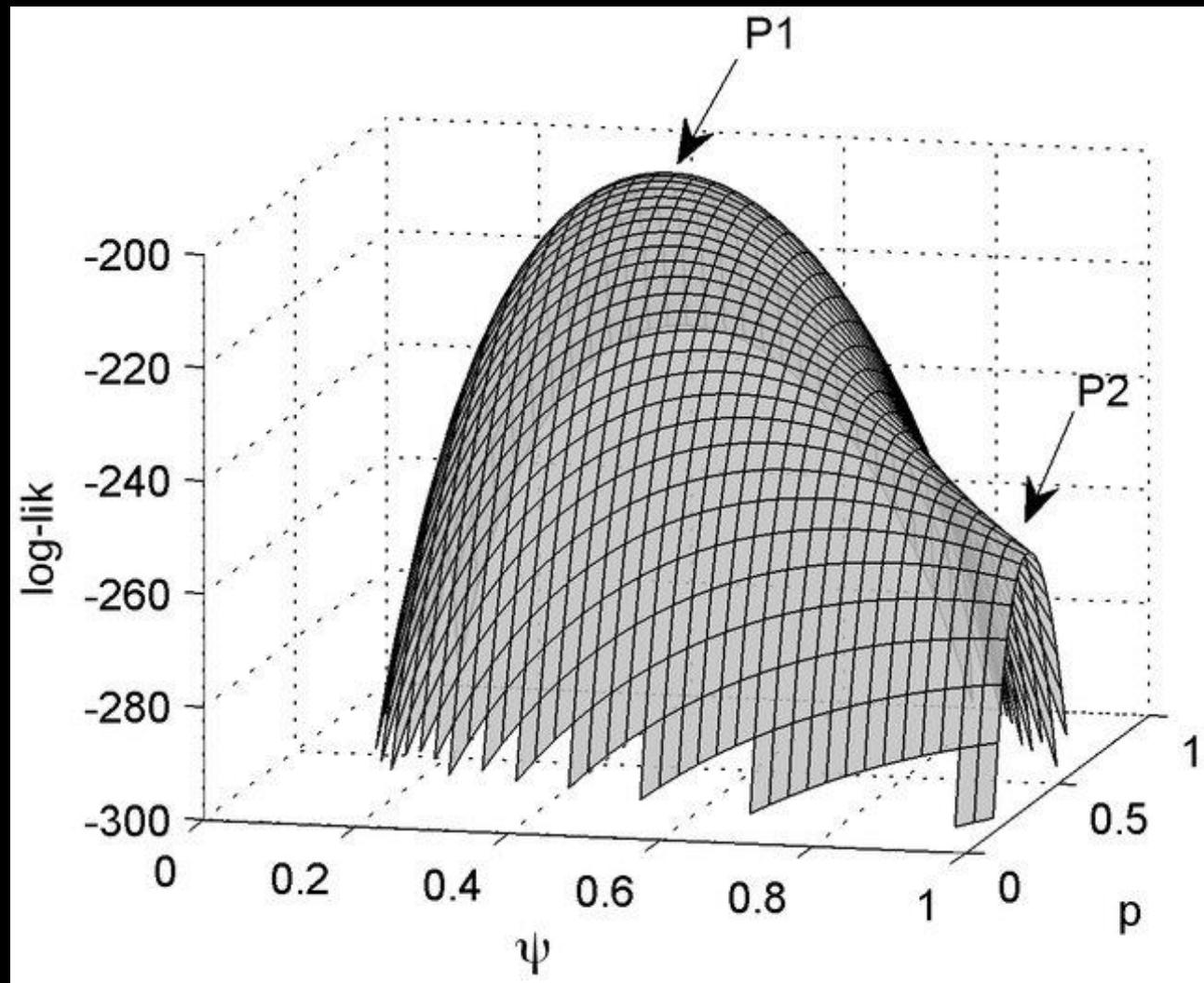
Input: data and phylogeny  
Automatic matching and tree pruning



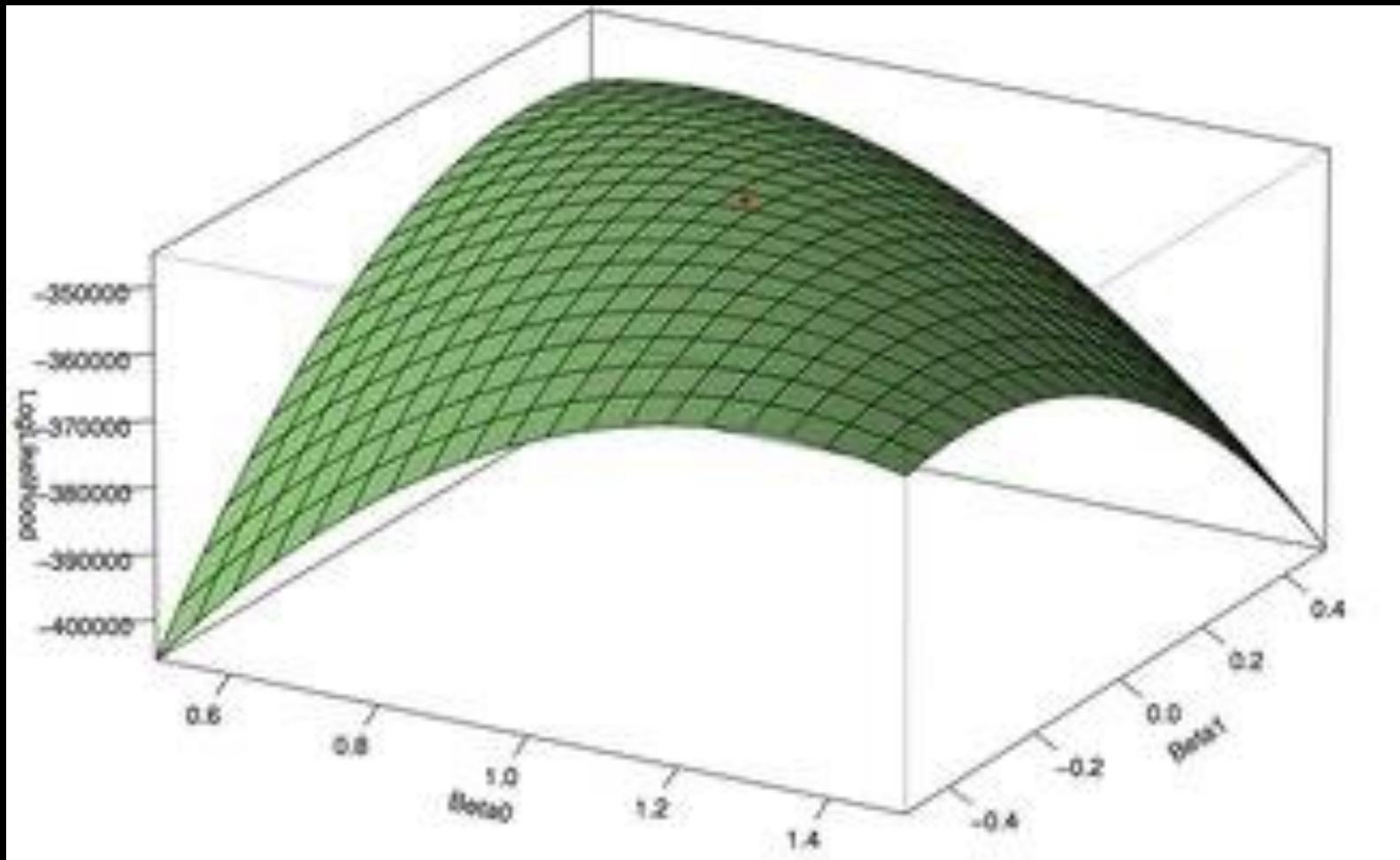
Common suffix: phylm (linear regression) | phyglm (logistic regression)  
physig (phylogenetic signal) | continuous (trait evolution) | discrete (trait evolution) | bd (diversification)  
Summary of the results: `summary( )` | Visualize the results: `sensi_plot( )`

# IDENTIFIABILITY ISSUES

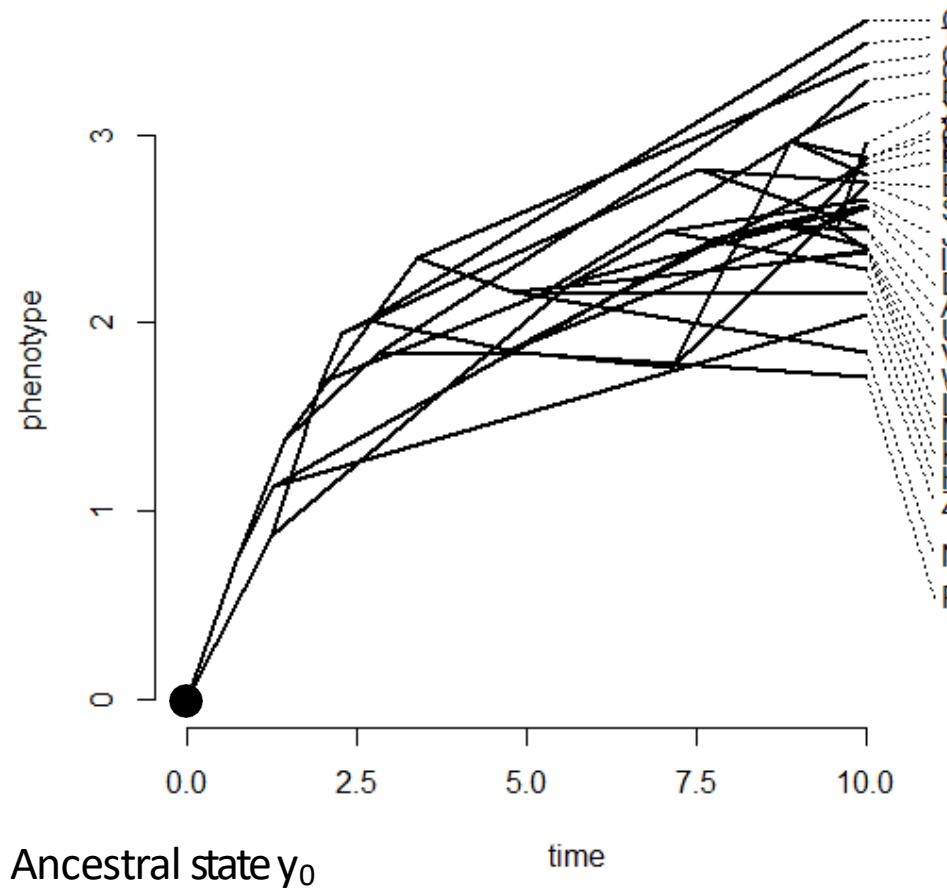
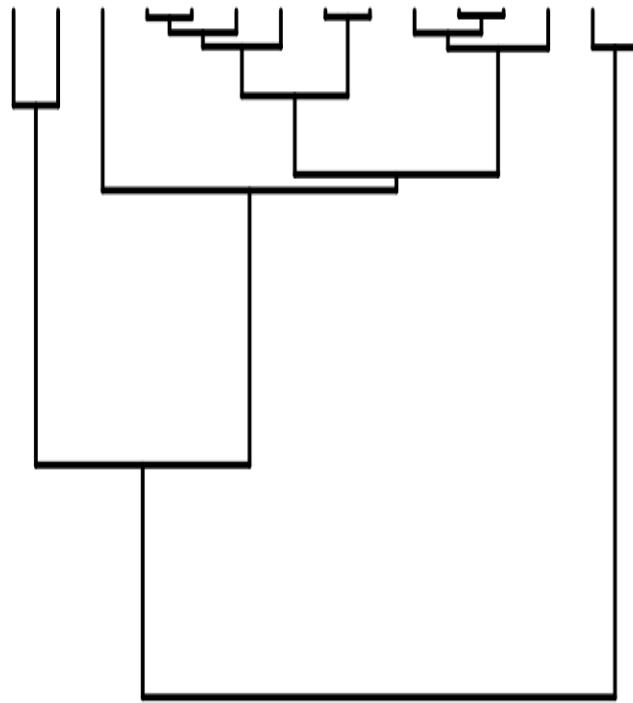
Sometimes model parameters  
interact with each other



Parameter estimation is an optimization procedure on a likelihood surface

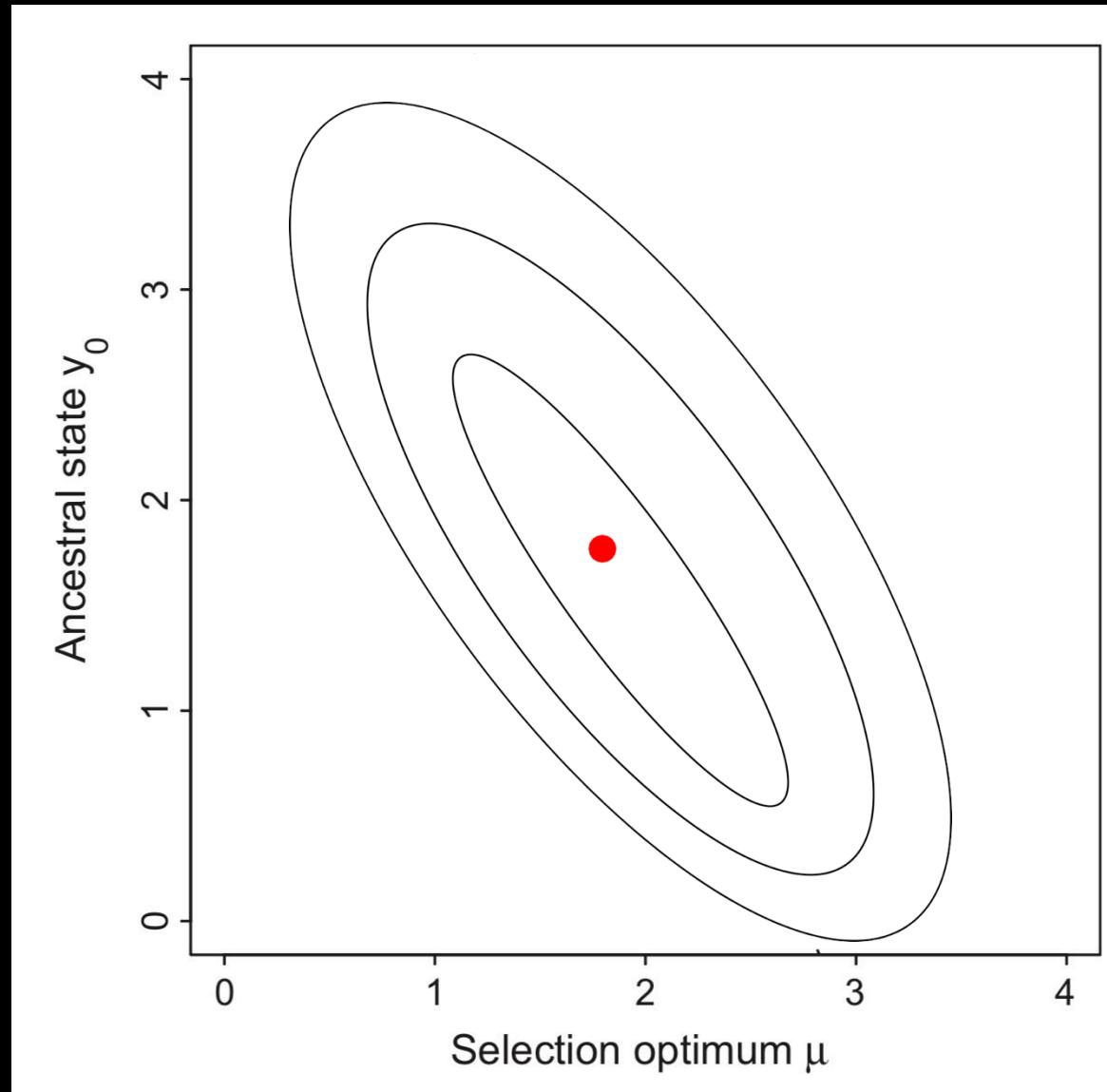


Sometimes likelihood surfaces can be flatter

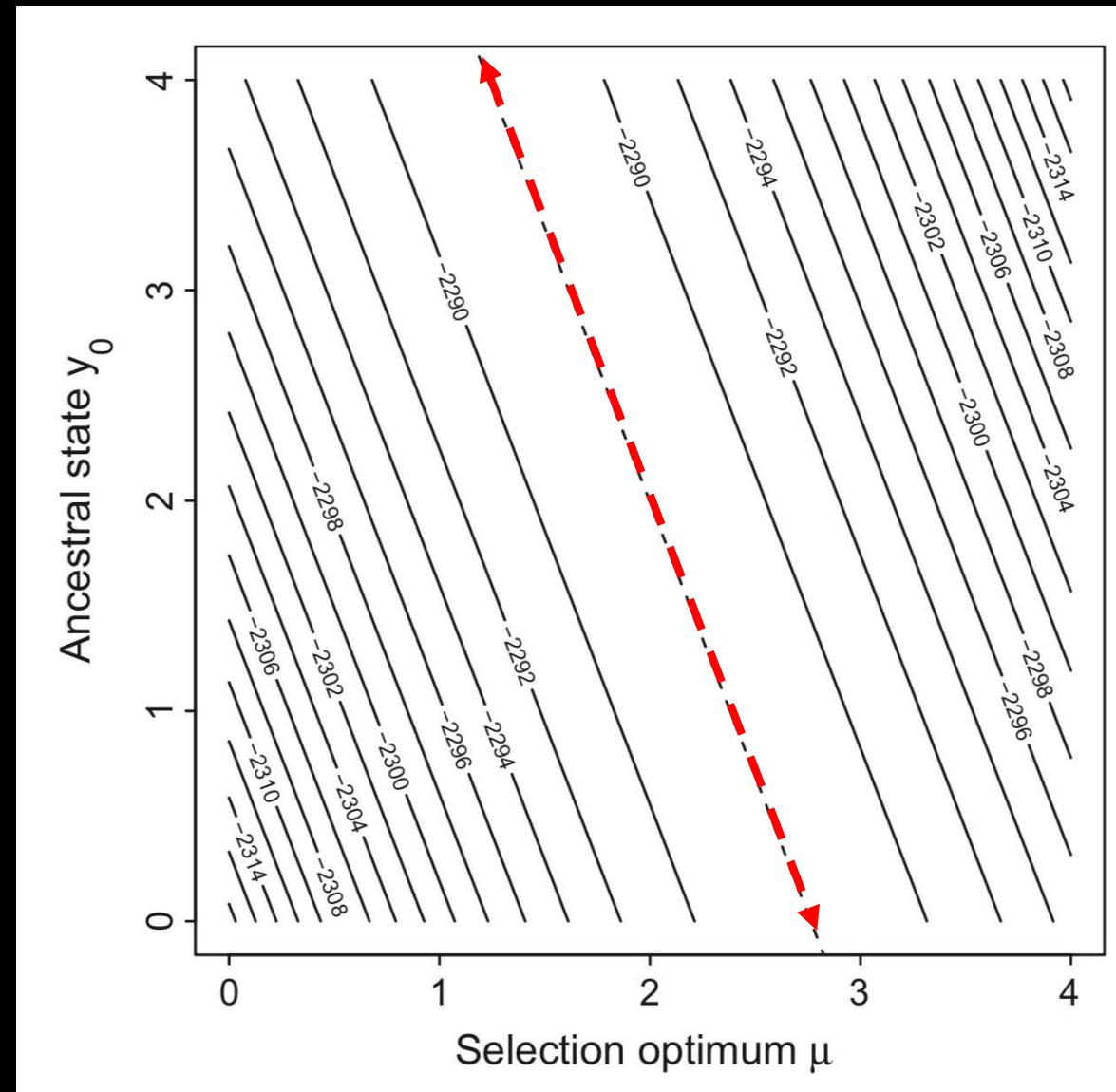


OU: OPTIMUM  $\mu$   
ANCESTRAL STATE  $y_0$

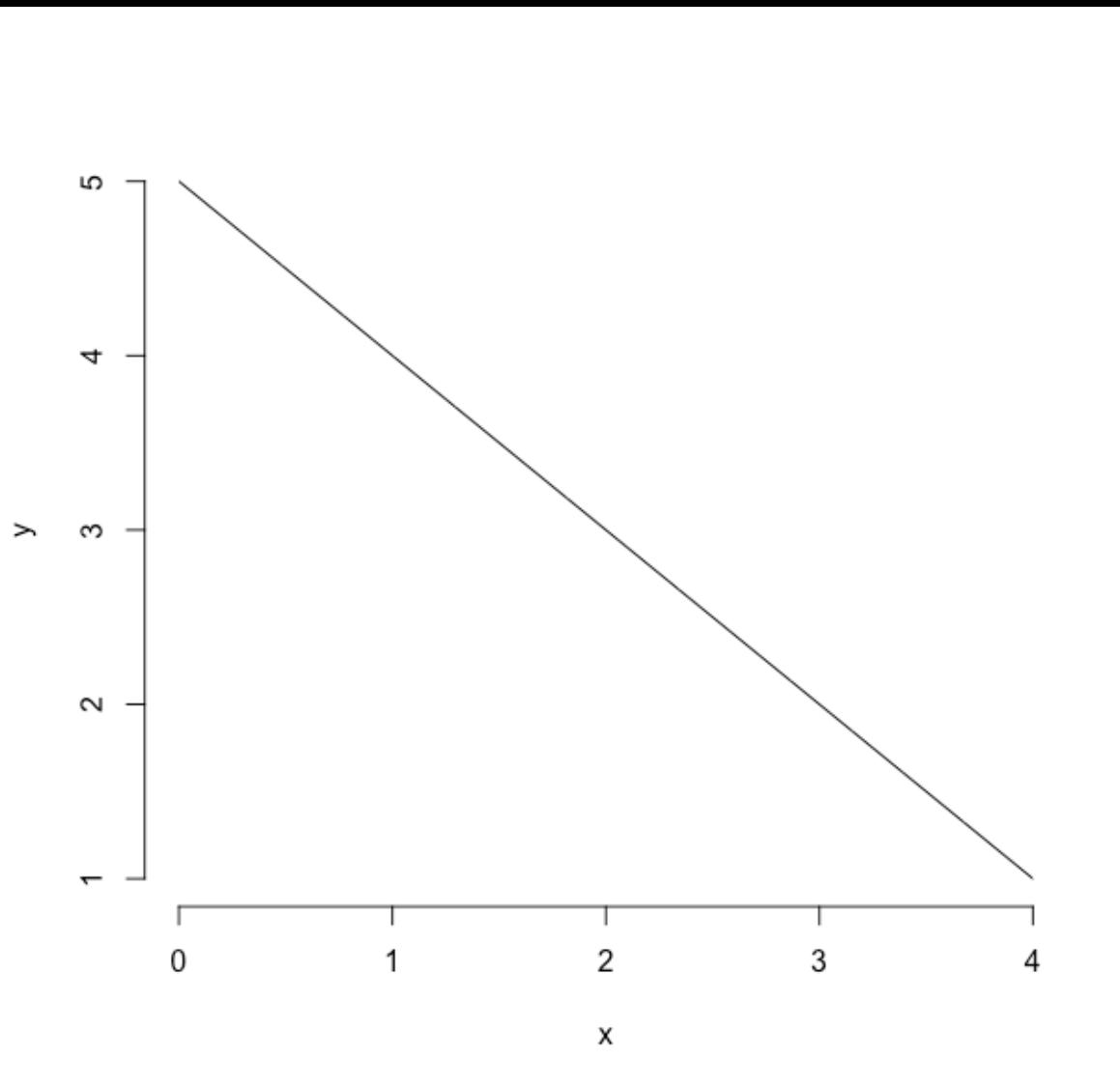
THIS IS WHAT WE WANT



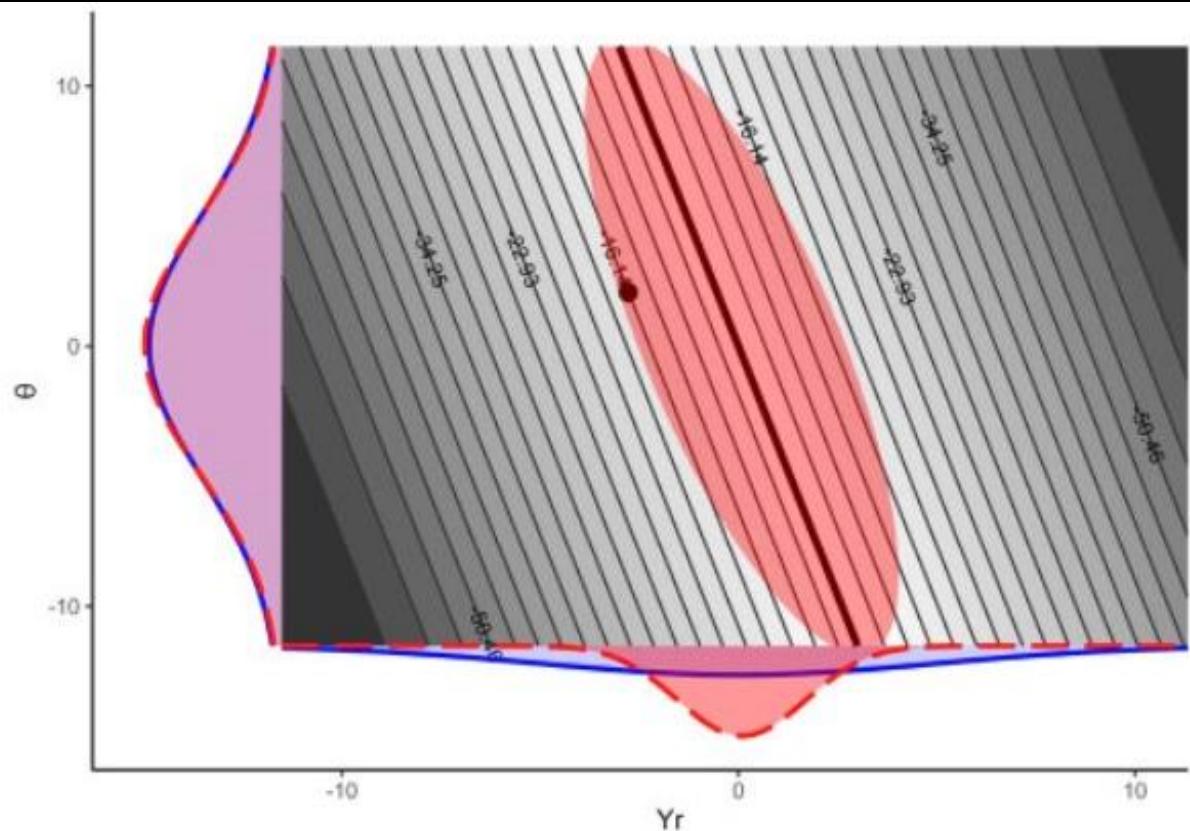
## THIS IS WHAT WE GET



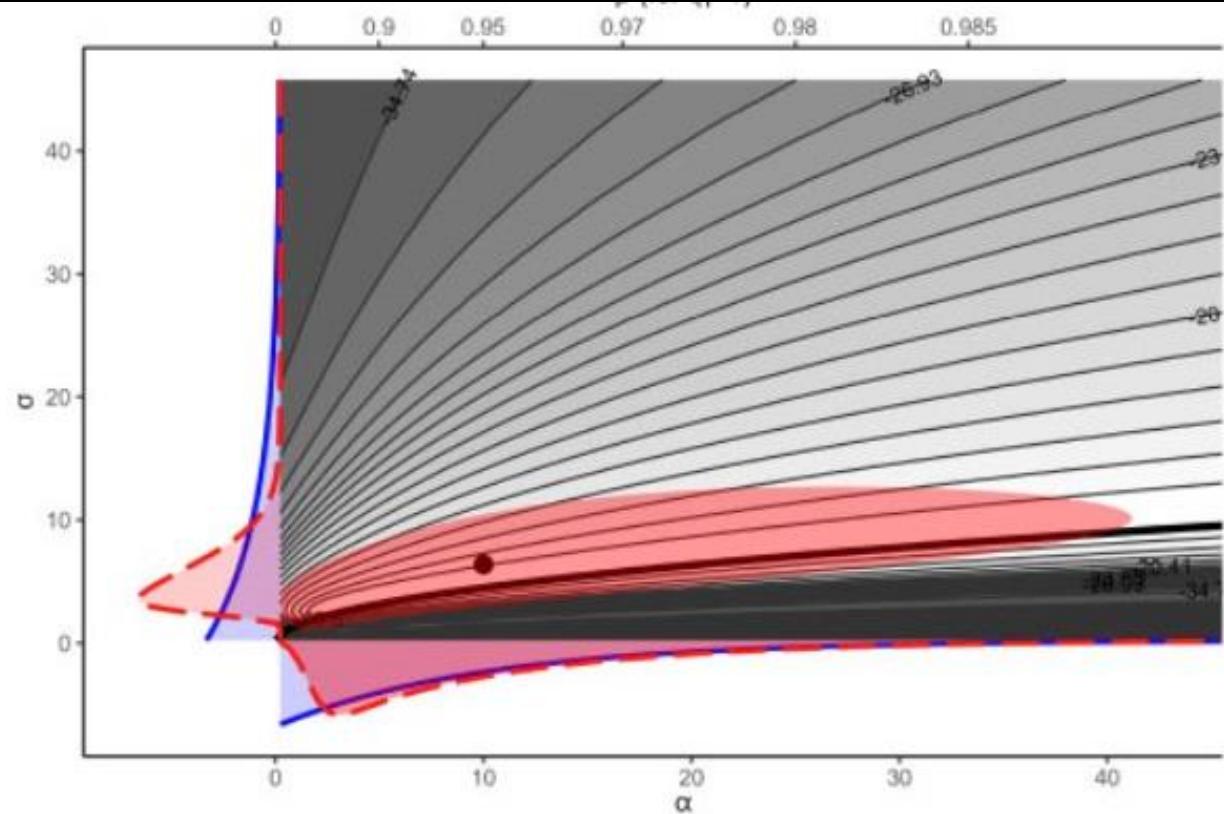
What is x in  $x+y=5$

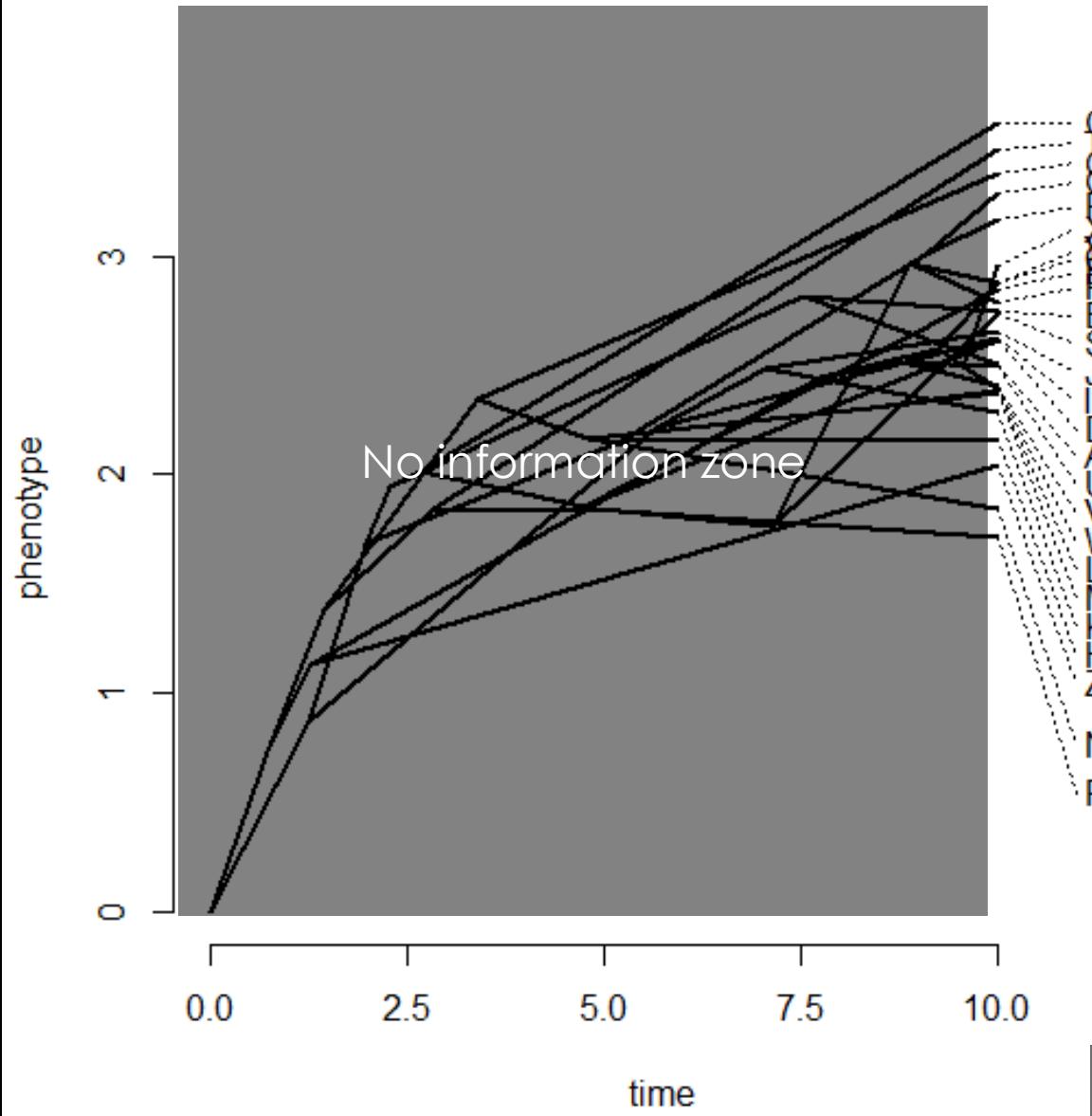


Theta and ancestral state

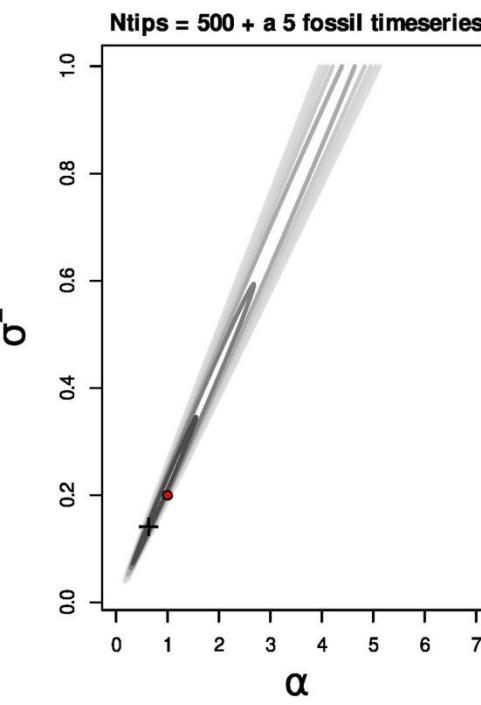
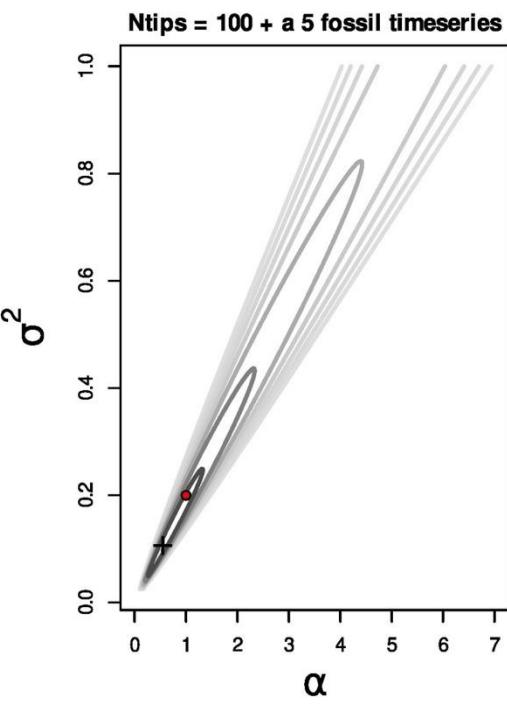
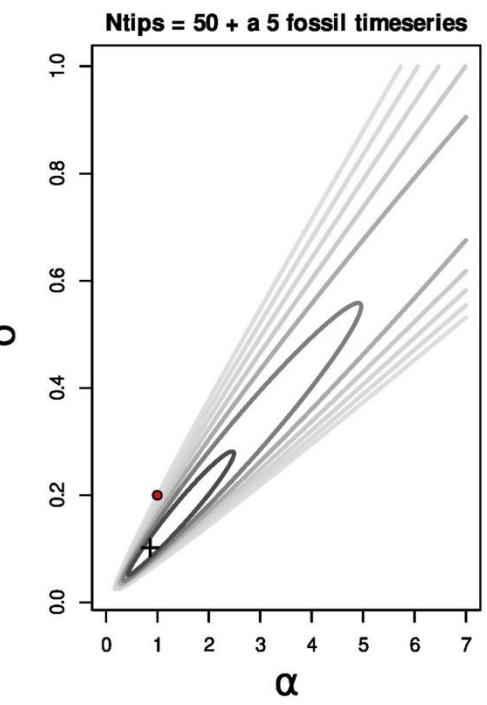
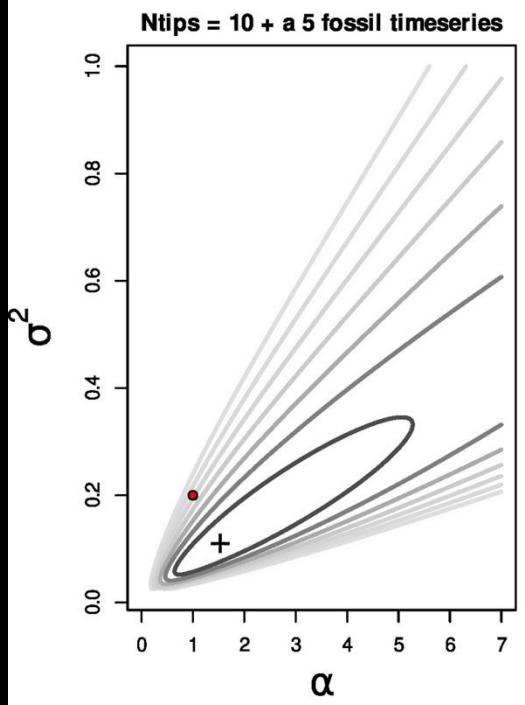
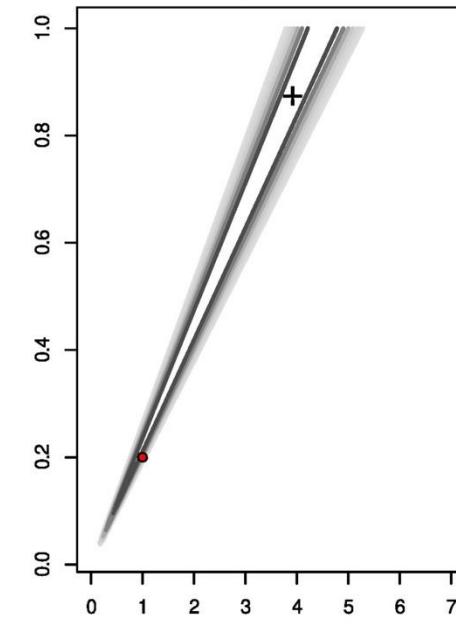
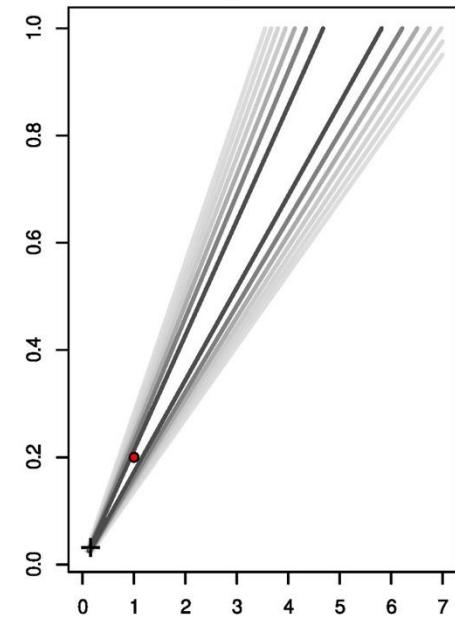
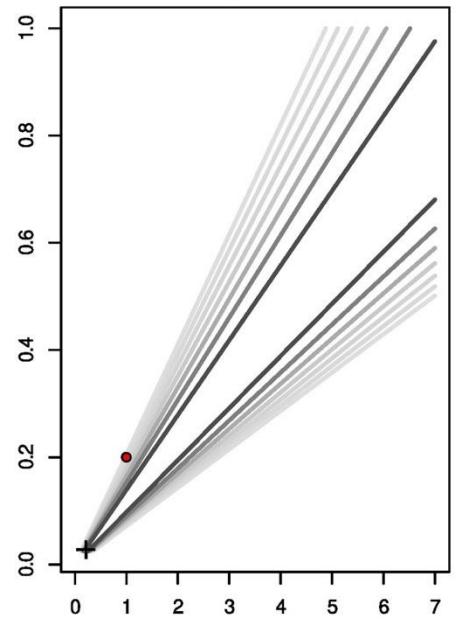
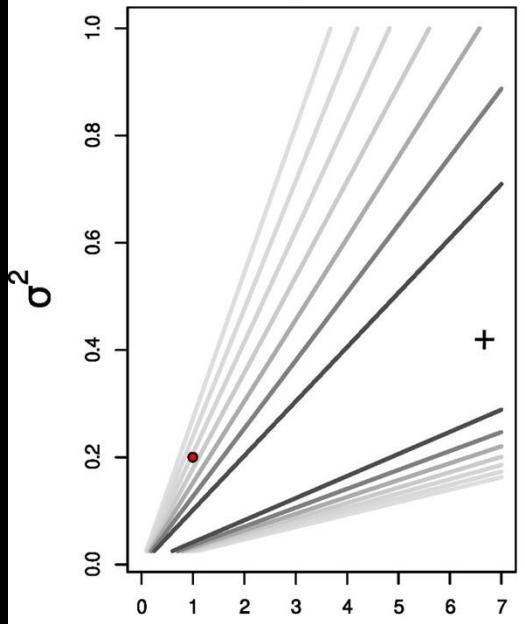


Alpha and rho





What can we do?



Add tips  
and  
fossils

# LESSONS

Always account for measurement error

Always account for phylogenetic uncertainty

Always account for parameter estimation error

Always account for model inadequacy

Always account for identifiability issues

# CAN REV BAYES SAVE US ALL?

measurement error

phylogenetic uncertainty

parameter estimation error

model inadequacy

identifiability issues

# CAN REV BAYES SAVE US ALL?

measurement error → not exclusively but yes

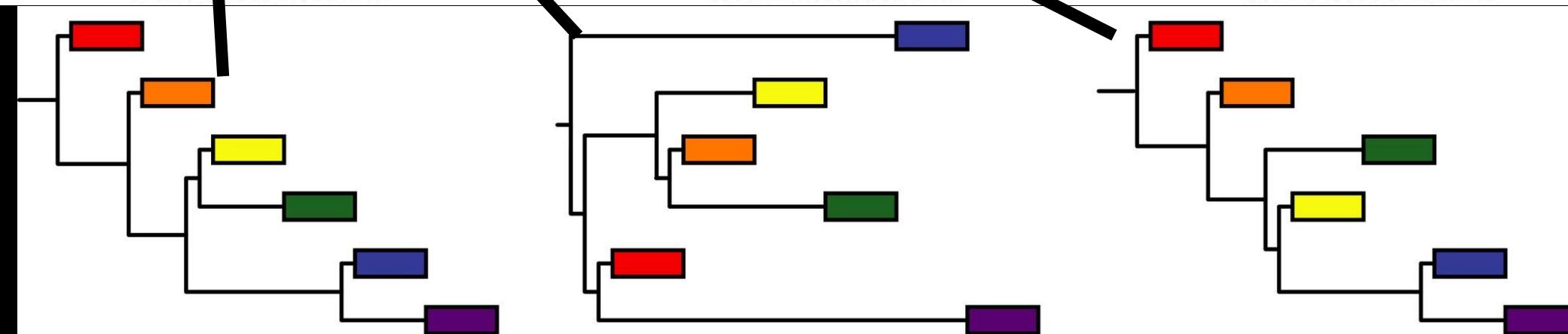
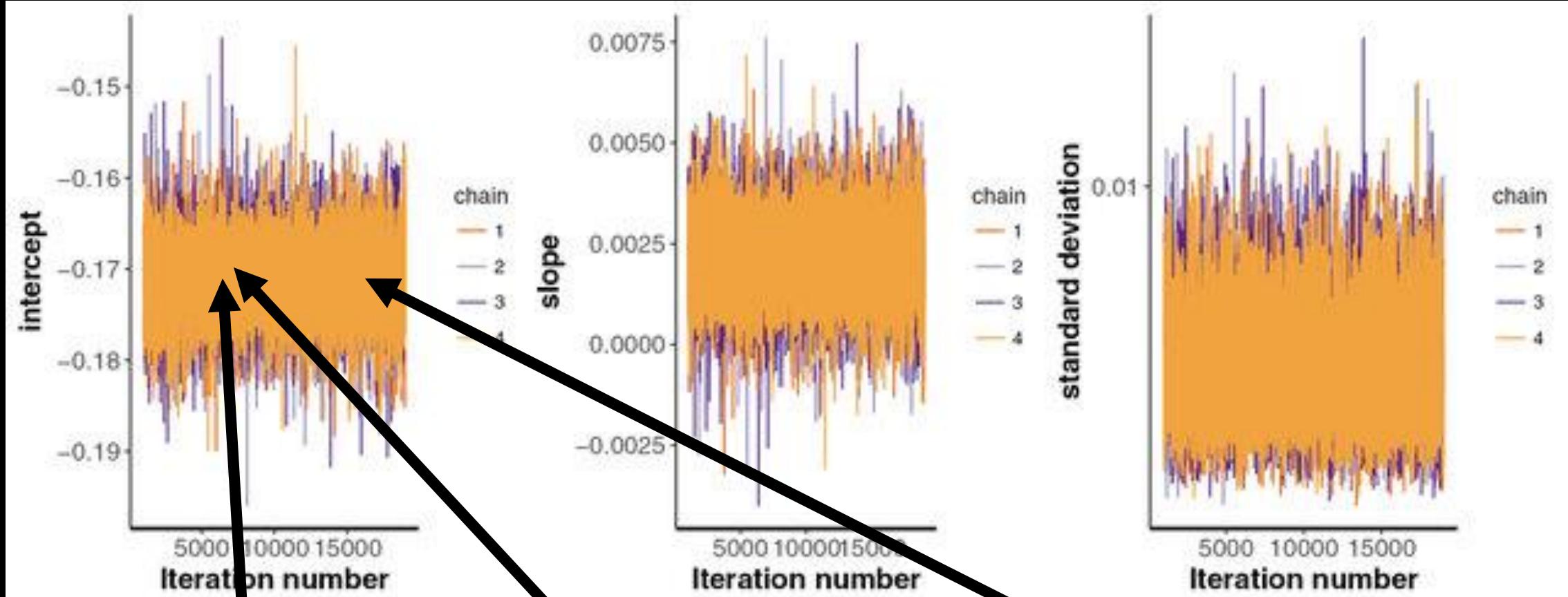
phylogenetic uncertainty →

parameter estimation error → yes

model inadequacy → no

identifiability issues → no

# The MCMC machinery can incorporate phylogenetic uncertainty



# CAN REV BAYES SAVE US ALL?

measurement error → not exclusively but yes

phylogenetic uncertainty → yes

parameter estimation error → yes

model inadequacy → no

identifiability issues → no